

B.Sc. (NAUTICAL SCIENCE)**Term-End Examination****June, 2011****BNA-011 : APPLIED MATHEMATICS***Time : 2 hours**Maximum Marks : 70*

Note : Attempt any five questions. Use of calculator is permitted.

1. (a) Find the angle between two vectors \vec{a} and \vec{b} having the same length $\sqrt{2}$ and their scalar products is -1 . 7

- (b) Evaluate $\int_0^1 \frac{dx}{1+x^2}$ using Simpson's $\frac{1}{3}$ rule 7

taking $h = \frac{1}{4}$

2. (a) A die is thrown 6 times. If "getting an odd number" is a "success", what is the probability of :

- (i) 5 successes
(ii) at least 5 successes

- (b) Obtain the line of regression of y on x for the data given below : 7
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|-------|-------|-------|-------|-------|-------|
| $x :$ | 1.53 | 1.78 | 2.60 | 2.95 | 3.42 |
| $y :$ | 33.50 | 36.30 | 40.00 | 45.80 | 53.50 |
3. (a) If $y = 3\cos(\log x) + 4\sin(\log x)$ show that $x^2y_2 + xy_1 + y = 0$. 7
- (b) If $y = (\tan^{-1}x)^2$ show that $(x^2 + 1)^2y_2 + 2x(x^2 + 1)y_1 = 2$. 7
4. (a) Evaluate $\int \sqrt{7x - 10 - x^2} \, dx$. 7
- (b) Find the area of the region included between the parabolas $y^2 = 4ax$ and $x^2 = 4ay$, where $a > 0$. 7
5. (a) In a spherical triangle ABC, angle $A = 124^\circ 21'$, side $AB = 41^\circ 30'$ and side $AC = 51^\circ 30'$. Calculate side BC using haversine formula. 7
- (b) In a spherical right angled triangle angle $B = 90^\circ$, angle $A = 43^\circ 30'$ and side $a = 41^\circ 45'$. Calculate sides b and c . 7

6. (a) Find the equation of the circle passing through the point $(2, 4)$ and centre at the intersection of the lines $x - y = 4$ and $2x + 3y = -7$. 7
- (b) Find the coordinates of the vertices, the foci, the eccentricity and the equations of the directrices of the hyperbola $16y^2 - 4x^2 = 1$. 7
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