

M.Sc. (MATHEMATICS WITH APPLICATIONS
IN COMPUTER SCIENCE)

M.Sc. (MACS)

Term-End Examination

December, 2010

00339

MMTE-007 : SOFT COMPUTING AND ITS
APPLICATIONS

Time : 2 hours

Maximum Marks : 50

Note : Attempt **any four** questions from Q. No. 1 to Q. No. 6
and Q. No. 7 is **compulsory**. Calculator are **not** allowed.

1. (a) Write the output function, of a neuron for 5
the following functions.

- (i) Linear transfer function.
(ii) Log - sigmoid transfer function.
(iii) Tan - sigmoid transfer function.

Also draw the graph of the output functions
of these transfer functions.

- (b) Let the universe of discourse U be given by 5

$$U = \{ 20, 21, 22, \dots, 25 \}$$

Let A be the fuzzy set defined on U by

$$A = \left\{ \frac{.5}{20}, \frac{.6}{21}, \frac{.7}{22}, \frac{.7}{23}, \frac{.9}{24}, \frac{1}{25} \right\}$$

- (i) Find A^c .
(ii) Draw the graph of A^c .

2. (a) What do you mean by a feed - forward neural network ? Using diagrams, show how it differs from a recurrent neural network. 6

(b) Consider a travelling sales man problem (TSP) involving eight cities A, B, C, D, E, F, G, H. A scheduling GA with various types of cross over operator is to be used to solve this TSP. Determine children solution of the following two parents using order cross over #1, assuming 2 - nd and 6 - th sites as the cross over sites. 4

Parent 1 : A B C D E F G H

Parent 2 : C A D B F H E G

3. (a) Draw the graph of the decision boundaries of MADALINE to solve XOR problems. 4

(b) Let R and S be defined on 4

$\{1, 3, 5\} \times \{1, 3, 5\}$ by

$R = \{(x, y) \mid y = x + 2\}$ and

$S = \{(x, y) \mid x < y\}$.

(i) Write the fuzzy relation matrices R and S.

(ii) Compute $R \circ S$ and $S \circ R$ using max - min composition.

(c) For the fuzzy set

2

$$A = \{(1, 0.2), (2, 0.5), (3, 0.8), (4, 1), (5, 0.7)\}$$

Find the α -cut of A for $\alpha = 0.5$.

4. Consider a data set of three points given in the following table, each of which has two features f_1 and f_2 . 10

| | f_1 | f_2 |
|-------|-------|-------|
| x_1 | 2 | 10 |
| x_2 | 4 | 9 |
| x_3 | 7 | 12 |

Assuming the values of the parameters c and m as 2 and the initial cluster centers $V_1 = (2, 2)$ and $V_2 = (5, 5)$, apply the FCM algorithm to find the new cluster center after one iteration.

5. (a) Consider the following population of binary strings for a maximization problem. 8

| | | | | | | |
|---------|--------|--------|--------|--------|--------|--------|
| String | 000101 | 010101 | 110000 | 101010 | 011011 | 100001 |
| Fitness | 2 | 5 | 1 | 10 | 8 | 20 |

Reproduce it using :

- (i) Tournament selection using tournament of size 2.
- (ii) Elitism.
- (b) Differentiate between supervised and unsupervised learning with the help of an example. 2

6. (a) If $\alpha_1 < \alpha_2$, then show that $A_{\alpha_1} \supseteq A_{\alpha_2}$, 3
 where \supseteq denotes the crisp superset relation.
 Illustrate this with an example.
- (b) Consider the ADALINE filter with three 5
 neurons in the input layer having weights
 $W_{11} = 3$, $W_{12} = 1$ and $W_{13} = -2$ and the
 input sequence
 $\{-, _, _, _, 0, 0, 0, -4, 5, 0, 0, 0, _ \}$.
 What is the filter output ?
- (c) Describe the following operators with 2
 suitable example for a GA.
 (i) Cross over. (ii) Mutation
7. Which of the following statement are true and
 which are false. Justify your answer. 2x5=10
- (a) If a single layer neural network has six
 inputs and two outputs, then six neurons are
 required.
- (b) The Hopfield network is a multi-layer neural
 network.
- (c) If A and B are two fuzzy sets where
 $\mu_A(x) = 0.3$, $\mu_B(x) = 0.9$ then
 $\mu_{C_{A \cup B}}(x_c) = 0.6$.
- (d) A set partition of a fuzzy set is a constrained
 soft partition only if $\sum_j \mu_{c_j}(x_i) < 1 \forall x_i \in X$.
- (e) The order of the schema ** 10 ** is 6.