Diploma in Civil Engineering / Diploma in Electrical & Mechanical Engineering

Term-End Examination December, 2010

BET-011: MATHEMATICS-I

Time: 2 hours Maximum Marks: 70

Note: Question number 1 is compulsory. Attempt any four more questions out of the remaining questions numbered 2 to 6. Use of calculator is permitted.

1. Answer *any seven* of the following :

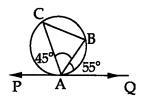
7x2 = 14

- (a) Convert $2 \times \sqrt[3]{4}$ as a pure surd of order 6.
- (b) If the lines 3y-2x=4 and 4y-px=2 are perpendicular, find the value of p.
- (c) Without solving, comment upon the nature of the roots of the equation $2x^2 + 8x + 9 = 0$.
- (d) Without using log tables, prove that $3 \log_{10}(1.5) + \log_{10}(240) 2\log_{10}9 = 1$
- (e) Find the sum of first 51 terms of the A.P. whose second and third term are 14, 18 respectively.
- (f) Find the principal value of $\csc^{-1}(-1)$.

(g) What is the meaning of the following box in a flow chart?



(h) In the figure given below, PQ is a tangent to the circle. If $\angle BAQ = 55^{\circ}$ and $\angle BAC = 45^{\circ}$, find $\angle ABC$.



(i) Find the eccentricity of the hyperbola $3x^2 - y^2 = 4$.

(j) If
$$\overrightarrow{a} = 2\overrightarrow{i} + \overrightarrow{j} - \overrightarrow{k}$$
 and $\overrightarrow{b} = \overrightarrow{i} - \overrightarrow{j} + 3\overrightarrow{k}$
find $3\overrightarrow{a} \cdot (\overrightarrow{a} + \overrightarrow{b})$.

(a) Without using trigonometric tables, find the value of
 4, 4, 6

$$\frac{\cos^2 20^\circ + \cos^2 70^\circ}{\sin^2 20^\circ + \sin^2 70^\circ} + \sin^2 64^\circ + \cos 64^\circ \sin 26^\circ.$$

(b) Prove that $\cot \theta + \tan \theta = \csc \theta \sec \theta$.

- (c) A flag-staff stands on the top of a 5 m high tower. From a point on the ground the angle of elevation of the top of the flag staff is 60° and from the same point the angle of elevation of the top of the tower is 45°. Find the length of the flag-staff.
- 3. (a) Dot product of a vector 3i 5k, 2i + 7j and i + j + k are respectively -1, 6 and 5. Find the vector. 5, 5, 4
 - (b) Find the value of λ for which $a = \lambda i + 2j + k$ and b = 4i 9j + 2k are perpendicular.
 - (c) Find a vector of length 3 units and perpendicular to the vectors $3\vec{i} + \vec{j} 4\vec{k}$ and $6\vec{i} + 5\vec{j} 2\vec{k}$.
- 4. (a) The sum of four numbers in Geometric Progression is 60 and the Arithmetic mean between the first and the last is 18. Find the numbers. 5, 5, 4
 - (b) Use the Binomial theorem to evaluate $(99)^4$.

(c) Simplify
$$\left\{ \sqrt[3]{x^4y} \times \frac{1}{\sqrt[4]{x^2y^8}} \right\}^{-6}$$
.

- 5. (a) Find the co-ordinates of the foot of the perpendicular dropped from the point P (3, 1) to the line AB whose equation is 2x y = 3. 5, 5, 4
 - (b) If a line passes through the point (1, 2) and cuts off positive intercepts on the *x*-axis and *y*-axis in the ratio of 2 : 3, find the equation of the line.
 - (c) Find the equation of the circle with centre (1, 3) and touching the line 3x + 4y + 5 = 0.
- 6. (a) Find the equation of an ellipse whose focus is (1, 0), the directrix is x + y + 1 = 0 and eccentricity is $\frac{1}{\sqrt{2}}$. 5, 5, 4
 - (b) In a triangle ABC, if a = 40, $c = 40\sqrt{3}$ and $B = 30^{\circ}$, solve the triangle.
 - (c) The length of a hall is 5m more than its breadth. If the area of the floor of the hall is 84 m², find the length and breadth of the hall.