

**DIPLOMA - VIEP - COMPUTER SCIENCE AND
ENGINEERING (DCSVI)**

Term-End Examination

00434

June, 2015

**BICS-033 : NUMERICAL METHODS AND
COMPUTATION**

Time : 2 hours

Maximum Marks : 70

Note : Attempt any five questions. Question no. 1 is compulsory. Each question carries equal marks. Calculator is allowed.

1. (a) If $f(x)$ is continuous in a closed interval $[a, b]$ and $f(a), f(b)$ are of opposite signs, then the equation $f(x) = 0$ will have at least _____ between a and b . $7 \times 2 = 14$
- (i) Four real roots
(ii) Two real roots
(iii) One real root
(iv) Three real roots
- (b) Bisection method is also called _____ method.
- (c) Regula Falsi method and Bisection method are somewhat similar. (True/False)

- (d) Method of successive approximation is also called _____ method.
- (e) Newton-Raphson method is referred to as the _____ .
- (f) When an approximate value of a root of an equation is given, a better and closer approximation to the root can be found using _____ method.
- (g) Regula Falsi method is also known as the method of false position. (True /False)

2. Find a root of the equation $x^3 - x - 11 = 0$ correct to four decimals using bisection method. 14

3. (a) Solve the system of equations $3x + y - z = 3$, $2x - 8y + z = -5$, $x - 2y + 9z = 8$, using Gauss elimination method. 7

(b) Solve the following system by the method of triangularisation : 7

$$2x - 3y + 10z = 3, -x + 4y + 2z = 20 \text{ and } 5x + 2y + z = -12.$$

4. Solve by Gauss-Seidel method, the following system of equations : 14

$$28x + 4y - z = 32, \quad x + 3y + 10z = 24 \text{ and } 2x + 17y + 4z = 35.$$

5. Find a polynomial which takes the following values :

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| | | | | | | |
|----------------|---|----|----|----|----|----|
| x | 1 | 3 | 5 | 7 | 9 | 11 |
| y _x | 3 | 14 | 19 | 21 | 23 | 28 |

and hence compute y_x at $x = 2, 12$.

6. Evaluate $\int_0^{10} \frac{dx}{1+x^2}$ by using

14

- (a) Trapezoidal Rule.
- (b) Simpson's 1/3 Rule.
- (c) Simpson's 3/8 Rule.

7. Solve $\frac{dy}{dx} = x + z$, $\frac{dz}{dx} = x - y^2$ with $y(0) = 2$, $z(0) = 1$ to get $y(0.1)$, $y(0.2)$, $z(0.1)$ and $z(0.2)$, approximately, by Taylor's algorithm.

14

8. Explain any *four* of the following :

$4 \times 3 \frac{1}{2} = 14$

- (a) Relative Error in Numerical Computation
- (b) Linear Programming
- (c) Golden Section Search
- (d) Trapezoidal Rule
- (e) Runge-Kutta Method for 4th Order
- (f) Secant Method