

**BACHELOR OF COMPUTER APPLICATIONS
(BCA) (Pre-Revised)**

01363 **Term-End Examination**

June, 2015

CS-73 : THEORY OF COMPUTER SCIENCE

Time : 3 hours

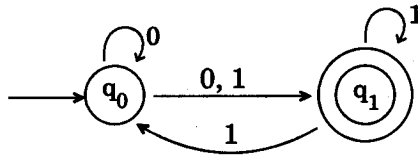
Maximum Marks : 75

Note : Question number 1 is compulsory. Attempt any three questions from the rest.

1. (a) Give the regular expression for the strings $\{a^2, a^5, a^8, \dots\}$. 2
- (b) List three applications of Finite Automata. 3
- (c) Briefly describe a Non-Deterministic Turing Machine. 5
- (d) Tabulate Chomsky hierarchy of grammar with an example for each. 5
- (e) Construct FA for the language $L(m) = \{aa, bb, aabb, aaaabbbb, \dots\}$. 5
- (f) Using parse tree, verify whether the following grammar is ambiguous or unambiguous :
 $S \rightarrow aSa \mid bSb \mid a \mid b \mid \epsilon$ 5
- (g) Show that if L and M are regular languages, then $L \cap M$ is also regular. 5

2. (a) Derive the equivalent FA from the following NFA :

5



- (b) Convert the following regular expression into a FA :

5

$(aa)^* a (bb)^*$

- (c) Give regular expression for all strings that do not end with ab.

5

3. (a) Show that the language

$L = \{ a^n b^n a^n : n \geq 0 \}$ is not regular.

5

- (b) Design a Turing Machine which multiplies the given binary input value by 2.

5

- (c) Explain in brief Universal Turing Machine.

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4. (a) Construct a PDA to accept

$L = \{ ww^R \mid w \in (0 + 1)^* \}$,

where w^R is reversed w .

5

- (b) Show that the language

$L = \{ a^{n^2} b^n : n \geq 0 \}$ is not context free.

5

- (c) Show that the predecessor function
 $\text{pred} : \mathbb{N} \rightarrow \mathbb{N}$ defined as

$$\text{pred}(n) = \begin{cases} 0 & \text{if } n=0 \\ n-1 & \text{if } n \geq 1 \end{cases}$$

is primitive recursive.

5

5. (a) Show that the state entry problem is undecidable.

4

- (b) If $f(x) = 2x^3 + 3x^2 + 1$

6

then show that

$$f(x) = O(x^4)$$

and also

$$f(x) \neq O(x^2).$$

- (c) Define the following :

5

(i) NP-Complete problem

(ii) NP-Hard problem