# MST-001 : FOUNDATION IN MATHEMATICS AND STATISTICS 

Time: 3 Hours
Maximum Marks : 50

Note: (i) Question No. 1 is compulsory.
(ii) Attempt any four questions from the remaining Question nos. 2 to 7.
(iii) Use of Scientific calculator (nonprogrammable) is allowed.
(iv) Use of Formulae and Statistical Tables

Booklet for PGDAST is allowed.
(v) Symbols have their usual meanings.

1. State whether the following statements are True or False. Give reason in support of your answer :

$$
5 \times 2=10
$$

(a) If $\mathrm{A}=\{0,1,2,3,4\},, \mathrm{B}=\phi$, then $\mathrm{A} \cup \mathrm{B}=\{\phi, 0,1,2,3,4\}$.
(b) The function $f(x)=x^{2}-6 x+2$ is minimum at $x=3$.
(c) If $A=\left[\begin{array}{l}4 \\ 5 \\ 6\end{array}\right]$ and $B=\left[\begin{array}{lll}4 & 5 & 6\end{array}\right]$, then $A B=\left[\begin{array}{lll}16 & 25 & 36\end{array}\right]$.
(d) The time in which an examinee completes the MST-001 paper come under discrete data.
(e) By using a histogram, one can find quartiles.
2. (a) Which term of the series $12,9,6, \ldots .$. is equal to -30 ?
(b) If the third term of a G. P. series is square of the first term and the fifth term is 64, find the series.
(c) If $A=\{1,2,3\}, B=\{2,3,4,5\}$ and

$$
\begin{aligned}
& C=\{2,4,6,8\}, \text { then verify that : } \\
& \qquad A \cap(B-C)=(A \cap B)-(B \cap C)
\end{aligned}
$$

(d) Find domain and range of the function

$$
\begin{equation*}
\left|x-\frac{1}{2}\right| . \tag{2}
\end{equation*}
$$

3. (a) Show that $\lim _{x \rightarrow 1} f(x)$ exists and is equal to $f(1)$, where :

$$
f(x)=\left\{\begin{array}{ccc}
x+1 & \text { for } & x \leq 1 \\
3-x^{2} & \text { for } & x>1
\end{array}\right.
$$

(b) Prove that:

$$
\left|\begin{array}{ccc}
1 & 1 & 1 \\
a & b & c \\
a^{2} & b^{2} & c^{2}
\end{array}\right|=(a-b)(b-c)(c-a)
$$

(c) Check the continuity of the function

$$
\begin{equation*}
\frac{|x-3|}{x-3} \text { at } x=3 \tag{4}
\end{equation*}
$$

P. T. O.
4. (a) A company has examined its cost structure of manufacturing a certain article and has determined that the total cost (C) and the number of articles ( $x$ ) manufactured are related as :

$$
C=5+\frac{48}{x}+3 x^{2}
$$

Find minimum value of C
(b) Given the matrices $\mathrm{A}, \mathrm{B}$, and C , where : 3

$$
A=\left[\begin{array}{ccc}
2 & 3 & -1 \\
3 & 0 & 2
\end{array}\right], B=\left[\begin{array}{l}
1 \\
1 \\
2
\end{array}\right] \text { and } C=[1-2]
$$

Verify that :

$$
(\mathrm{AB}) \mathrm{C}=\mathrm{A}(\mathrm{BC})
$$

(c) A sample of 40 PGDAST learners answered the following questions asked in a survey:
(i) What is your gender?
(ii) What is your age?
(iii) What is your current major area of study?
(iv) What is your percentage of marks in graduation?
(v) What is your current employment status?
(vi) How many different jobs have you held in the past 10 years?

For each of the question mentioned above determine whether the data thus obtained come under nominal, ordinal, interval and ratio scale. Give reason in support of your answer.
5. (a) Represent the following information of the average marks of PGDAST learners by a suitable diagram :

| Year | Average marks |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | MST-001 | MST-002 | MST-003 | MST-004 |
| 2016 | 78 | 65 | 70 | 60 |
| 2017 | 82 | 60 | 72 | 62 |

P. T. O.
(b) The data given below represents the total fat (in grams per serving) for a sample of 16 chicken sandwiches from fast-food chains :
$7,8,4,5,16,20,20,24,19,30,23,20,19$, 30, 35, 6

Construct a box plot for the above data. 6
6. (a) In an examination of statistics, a candidate has to select 7 questions from three different groups A, B and $C$, which contains 3, 4, 4 questions respectively. In how many different ways can a candidate select at least 2 questions from each group ?
(b) How many different signals are possible with 3 red, 4 white and 2 green flags by using all at a time in a queue ?
(c) Find $\frac{d y}{d x}$, where :

$$
y=\frac{x^{2}-1}{x^{2}+1}
$$

7. (a) Find: $\int_{0}^{6} f(x) d x$

$$
\text { where } f(x)=\left\{\begin{array}{cc}
x^{2}+3 & 0 \leq x<3 \\
2 \sqrt{x} & 3 \leq x<4 \\
e^{-x}-e^{-2 x} & 4 \leq x \leq 6
\end{array}\right.
$$

(b) The following data represent the electricity bill (in ₹) during July 2017 for a random sample of 25 one-bedroom apartments in a metro city :

696, 660, 890, 780, 1000, 1150, 900, 660,
850, 800, 1100, 700, 740, 820, 970, 900, $750,780,600,700,750,1010,690,760,800$
(i) Form a frequency distribution by taking class intervals as 600-700, 700-800,
(ii) Construct a histogram.
(iii) Construct ogives.
(iv) Find median with the help of ogives.

