

B.Sc. (NAUTICAL SCIENCE)

Term-End Examination

June, 2014

BNA-011 : APPLIED MATHEMATICS

Time : 2 hours

Maximum Marks : 70

*Note : (i) Attempt any five questions.**(ii) Use of scientific calculator is allowed.*

1. (a) If $\bar{a} = 6\hat{i} - \hat{j} + 7\hat{k}$ and $\bar{b} = 2\hat{i} - \hat{j} + \lambda\hat{k}$ find the value of λ such that $(\bar{a} + \bar{b})$ and $(\bar{a} - \bar{b})$ are orthogonal vectors. 7

- (b) Find $\int_0^{20} f(x)dx$, where $f(x)$ is given by the following table, using Simpson's one-third rule. 7

$x :$	0	2	4	6	8	10	12	14	16	18	20
$f(x) :$	0	10	18	25	29	32	20	11	5	2	0

2. (a) The probability that a fire accident due to short circuit is 0.8 and due to the LPG cylinder explosion is 0.2. Chance of fire accident is 30% given a short circuit and 95% given on LPG explosion. Based on these, what do you think is the most probable cause of fire? Statistically justify your answer. 7

- (b) Find the mean and standard deviation of the following data : 7

x	132 -136	136 -140	140 -144	144 -148	148 -152
f	5	6	27	8	4

3. (a) If $y = x^x + (\sin x)^x$ find $\frac{dy}{dx}$ 7

- (b) If $x = a \cos t$, $y = a \sin t$ find $\frac{d^2y}{dx^2}$ at $t = \frac{\pi}{4}$. 7

4. (a) Evaluate $\int \frac{x + 27}{x^2 - 9} dx$ 7

- (b) Using integration find the area of the region bounded by the curve $x^2 = 4y$ and the line $x = 4y - 2$. 7

5. (a) In a spherical triangle LMN angles L and M are 90° and $44^\circ 16.0'$ and the side m is $39^\circ 37'$. Calculate side n. 7

- (b) In a quadrantal spherical triangle PZX $P = 90^\circ$, $x = 64^\circ$ and $Z = 90^\circ$. Calculate X. 7

6. (a) Find the equation of ellipse if the length of latus rectum is $\frac{5}{2}$ and $e = \frac{1}{2}$. 7

- (b) Find the equation of the circle passing through the points $(-2, 1)$ and $(1, -2)$ and having the center on the line $x + y + z = 0$. 7