

**B.Tech. MECHANICAL ENGINEERING
(BTMEVI)**

**Term-End Examination
June, 2013**

BIMEE-013 : FINITE ELEMENT ANALYSIS

00017

Time : 3 hours

Maximum Marks : 70

Note : Answer any five questions. Scientific calculator is allowed. All questions carry equal marks.

1. (a) Explain the basic steps of Rayleigh-Ritz method. 6
- (b) Why polynomial terms preferred for shape functions in FEM ? 6
- (c) Define the term 'Stiffness Matrix'. 2

2. A beam AB of span ' l ' simply supported at the ends and carrying a concentrated load ' W ' at the centre ' C ' as shown in Figure 1. Determine the deflection at the mid span using Rayleigh-Ritz method and compare it with exact solution. Use a suitable one term trigonometric trial function. 14

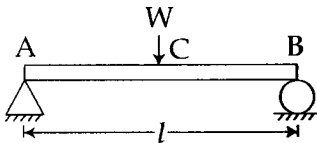
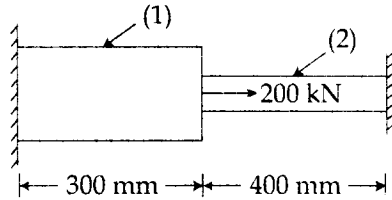


Figure - 1

3. A stepped bar, fixed both ends, is subjected to an axial load of 200 kN at the place of change of cross section as shown in figure 2. Find : 14
- The nodal displacements
 - The reaction forces
 - The induced stresses in each material.



(1) - Aluminium bar (2) - Steel bar

$$A_1 = 2400 \text{ mm}^2 \quad E_1 = 70 \times 10^3 \text{ N/mm}^2$$

$$A_2 = 600 \text{ mm}^2 \quad E_2 = 200 \times 10^3 \text{ N/mm}^2$$

Figure - 2

4. Consider a 4- bar truss as shown in figure 3. It is given that $E = 200 \text{ Gpa}$ and $A = 500 \text{ mm}^2$ for all the elements. Determine : 14
- Nodal displacements
 - Support reaction
 - Element stresses

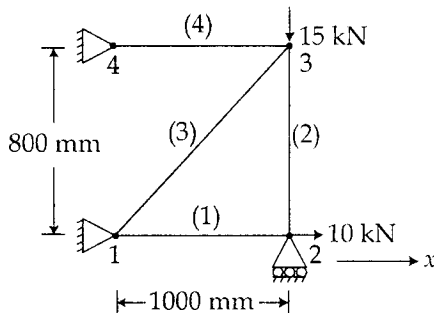


Figure - 3

5. Determine the deflection and stresses in three different sections of a composite stepped bar loaded as shown in the figure 4. 14

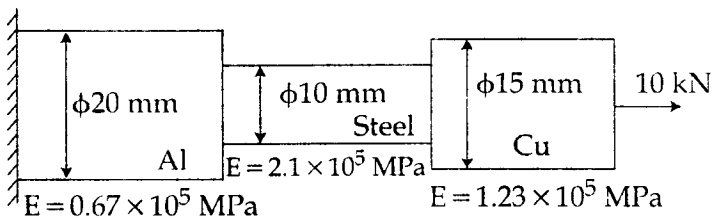


Figure - 4

6. (a) Use Hermite's interpolation formula to derive cubic shape functions for the transverse deflection of beams. 7
- (b) Derive the local finite element stiffness matrix for a beam with combined transverse loading and axial force. 7
7. Derive the shape functions for a beam finite element of length 'L' assuming a cubic polynomial in the form $v(x) = a_0 + a_1x + a_2x^2 + a_3x^3$ by satisfying the boundary conditions : 14
- $v(0) = 0$ and $v(L) = 0$,
- $v'(0) = 0$ and $v'(L) = 0$.
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