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**B.Tech. ELECTRICAL ENGINEERING
(BTELVI)**

Term-End Examination

June, 2013

BIEEE-015 : STOCHASTIC CONTROL SYSTEMS

Time : 3 Hours

Maximum Marks : 70

*Note : Attempt **any five** questions. All questions carries **equal** marks. Use of **scientific** calculator is allowed.*

1. Find the first order probability density $p(x, t)$ of the random process $x(t) = \cos(W_c t + y)$ **14**
Where y is a random variable with probability

$$\text{density } P_y(Y) = \begin{cases} 1/2\pi & \text{for } 0 \leq y \leq 2\pi \\ 0 & \text{otherwise} \end{cases}$$

2. Show that the output of a fixed-lag smoother driven from a Kalman filter with the smoother states instantaneously reset to zero (or some arbitrary values) at $k=j$ yield the correct fixed lag estimates for $k \geq j+N$. **14**
3. Show that a second order random variable is necessarily first order, but the converse need not be true. **14**

4. Verify that if F and G are two probability distribution function and $0 \leq \lambda \leq 1$, then $\lambda F + (1 - \lambda) G$ is also a probability distribution function. 14
5. When is a filter optimal ? Write in detail about Bounded Optimal filter. 14
6. Consider a deterministic SISO LTI system of the form $y_{k+1} = ay_k + bu_k$ 14
Where a and b are two unknown constants. Determine a and b , so that $\{u_k\}$ can be implemented on - line.
7. Write down four important characteristics of Basic filter and discuss each of these characteristics in detail. 14
8. Write notes on *any two* of the following : 7x2=14
- (a) Ballman dynamic programming method
 - (b) LQG optimal controls
 - (c) Gauss-Markov sequence model
 - (d) Wiener Process
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