

**B.Tech. ELECTRICAL ENGINEERING
(BT ELVI)**

Term-End Examination

June, 2013

BIEEE-002 : DIGITAL CONTROL SYSTEM

Time : 3 Hours

Maximum Marks : 70

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- Note : (1) Attempt any seven questions.
(2) Each question carry equal marks.*
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1. Define the properties of Z-transform related to : 10
 - (a) Shifting theorem (Left and Right)
 - (b) Initial and Final value theorem.

2. Find Z-transform of following : 10
 - (a) $\sin wt$
 - (b) $t u_s(t)$
 - (c) $t e^{at}$
 - (d) impulse function

3. Explain the specification of transient response in terms of Z - plane with suitable diagram. 10

4. Explain how to get the solution of non-homogeneous state equation. 10

5. Determine the stability of the system described by **10**

$x^\circ = Ax$, where $A = \begin{bmatrix} -1 & -2 \\ 1 & -4 \end{bmatrix}$ by the second method of Liapunov.

6. Explain the properties of state transition matrix **10**
 $Q(t)$. Obtain the $Q(t)$ for given equation.

$x^\circ = Ax$ where

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{bmatrix}$$

7. Write short note on : **10**

- (a) Bilinear transformation
(b) Routh stability criterion on the r plane.

8. (a) Define the concept of complete **10**
controllability and observability.

- (b) Check the controllability and observability

$$A = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix}, B = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

$$C = [1 \ 2]$$

9. Find optimal control **10**
 $u^\circ(k)$, $k = 0, 1, 2, \dots, 10$, Such that the performance

index $J = \frac{1}{2} \sum_{k=0}^{10} \{x^2(k) + 2u^2(k)\}$ is minimized.

Subject to the equality constraint

$$x(k+1) = x(k) + 2u(k)$$

initial state is $x(0) = 1$

final state is $x(11) = 0$

10. Derive the expression of Riccati equation.

10
