

**B.TECH. (AEROSPACE ENGINEERING)  
(BTAE)**

**Term-End Examination  
June, 2013**

**BAS-020 : BASIC CONTROL THEORY**

Time : 3 hours

Maximum Marks : 70

*Note : Attempt seven question in all. Question no.1 compulsory. Use of scientific calculator is permitted. All questions carry equal marks.*

1. Choose the correct or best answer in the following : 5x2=10

(a) Closed-loop transfer function of a unity-feed back system is given by

$$\frac{Y(s)}{R(s)} = \frac{1}{(\tau s + 1)}$$

Steady state error to unit-ramp input is :

- (i)  $\infty$
- (ii)  $\tau$
- (iii) 1
- (iv)  $1/\tau$

- (b) Electrical time constant of an armature controlled dc servomotor is :
- (i) equal to mechanical time constant
  - (ii) smaller than mechanical time constant
  - (iii) larger than mechanical time constant
  - (iv) none of the above
- (c) Peak overshoot of step-input response of an underdamped second-order system is explicitly indicative of :
- (i) settling time
  - (ii) rise time
  - (iii) natural frequency
  - (iv) damping ratio
- (d) A type-1 plant is changed to type-2 feedback system by the following cascade control action :
- (i) PD
  - (ii) PI
  - (iii) Either PD or PI
  - (iv) Neither PD nor PI
- (e) A unity feedback system has open-loop transfer function  $G(s) = \frac{K}{[s(1 + s\tau)]}$ .
- (i)  $\infty$
  - (ii) 0
  - (iii) 1
  - (iv) none of the above

2. Given the transfer function 10

$$G(s) = \frac{Y(s)}{R(s)} = \frac{1}{s^2 + 3s + 2}$$

Find the response  $y(t)$  to the input

- (a)  $r(t) = 5u(t)$   
(b)  $r(t) = 5tu(t)$

Find the steady-state component  $y_{ss}$  of  $y(t)$  in each case.

3. Obtain the roots of given characteristic polynomial 10  
on the basis of the Routh's array :

- (a)  $s^4 + 2s^3 + 11s^2 + 18s + 18 = 0$   
(b)  $s^6 + 3s^5 + 5s^4 + 9s^3 + 8s^2 + 6s + 4 = 0$

4. A unity-feedback system has open-loop transfer 10  
function

$$G(s) = \frac{W_n^2}{s(s + 2\zeta W_n)} ; (\zeta < 1)$$

Derive expressions for peak overshoot  $M_p$  and peak time  $t_p$  of the time response of the given system to unit-step input.

5. Consider a unity-feedback system with a forward 10  
path transfer function

$$G(s) = \frac{K(s + 3)}{s(s + 2)} ; K \geq 0$$

Show that root-locus circle is the part of the root locus. Construct the root locus and determine the damping ratio for maximum oscillatory response. What is the value of  $K$  at this point of the locus ?

6. (a) Using principle of argument, derive the Nyquist's stability criterion. 5x2=10  
 (b) Give an example of physical system whose transfer function model has a pole in the right-half s-plane.

7. Determine gain crossover frequency, phase crossover frequency, gain margin and phase margin of a feedback system with open loop transfer function 10

$$G(s) = \frac{40}{(s+2)(s+4)(s+5)} \text{ using bodeplots.}$$

8. The open-loop transfer function of a control system is : 10

$$G(s)H(s) = \frac{1}{s(1+0.5s)(1+2s)}$$

- (a) Determine approximate value of gain margin and phase margin.  
 (b) If a lag compensator with transfer function  $D(s) = \frac{K_c(1+3s)}{(1+5s)}$  is inserted in the forward path, find the value of  $K_c$  to keep the gain margin unchanged.
9. Write short notes on *any two* of the following : 2x5=10
- (a) Stability  
 (b) Proportional integral differential controller  
 (c) Computer electronic design aspects