

# B.TECH. IN COMPUTER SCIENCE AND ENGINEERING (BTCSEVI)

Term-End Examination

December, 2012

## BICS-018 : THEORY OF COMPUTATION

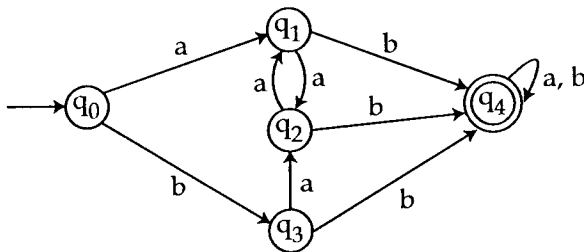
Time : 3 hours

Maximum Marks : 70

*Note : Attempt any seven questions.*

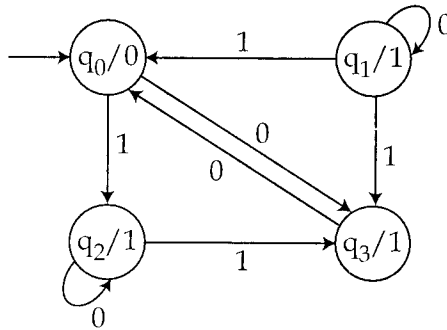
*All questions carry equal marks.*

1. (a) Design a finite automation to accept the language  $L$  over  $\{a, b\}$  such that  $L = \{a^n b^m \mid n, m \geq 0 \text{ and } n + m \text{ is even}\}$ . 5
- (b) Construct a minimum state automation equivalence to the following diagram. 5

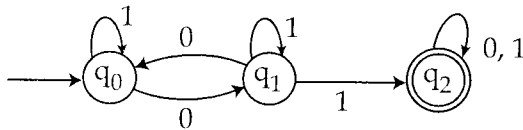


2. (a) Design Moore and Mealy machine to convert each occurrence of substring 100 by 101. 5

- (b) Differentiate between Mealy and Moore machine and convert following Moore machine into an equivalent Mealy machine 5



3. (a) Find the regular expression for the following diagram : 5



- (b) Construct a DFA for equivalent regular expression (RE)  $r = (01 + 2^*)^*1$ . 5
4. (a) Explain pumping lemma for regular expression and show that language  $L = \{a^n b^n c^n \mid n \geq 1\}$  is not regular. 5
- (b) Differentiate between Chomsky and Greibach Normal forms and convert the grammar 5
- $S \rightarrow ABb/a$   
 $A \rightarrow aaA/B$   
 $B \rightarrow bAb$  into GNF.

5. (a) Explain pumping lemma for context free language (CFL) and prove that the language  $L = \{O^K \mid K \text{ is a perfect square}\}$  is not a CFL. 5
- (b) Design a context free grammar (CFG) for the language  $L(G) = \{a^{2n} b^m \mid n \geq 0, m \geq 0\}$ . 5
6. (a) Differentiate between deterministic and non deterministic push down automata and explain equivalence between push down automata and context free grammars. 5
- (b) Design a Push Down Automata (PDA) for the language  $L = \{a^n b^n \mid n \geq 1\}$ . 5
7. (a) For the following PDA  $M$ , design the corresponding CFG  $G$ . 10
- $M = (\{q_0, q_1\}, \{0, 1\}, \{Z_0, K\}, \delta, q_0, Z_0, \phi)$  with transition function  $\delta$  as follows :
- $\delta(q_0, 1, Z_0) \vdash (q_0, K Z_0), \delta(q_0, 0, K) \vdash (q_1, K)$   
 $\delta(q_0, \epsilon, Z_0) \vdash (q_0, \epsilon), \delta(q_1, 0, K) \vdash (q_1, \epsilon)$   
 $\delta(q_0, 1, K) \vdash (q_0, KK), \delta(q_1, 0, Z_0) \vdash (q_0, Z_0)$
8. What is Turing Machine (TM) ? Design a Turing Machine (TM) which accept the string over  $\{0, 1\}$ , containing even number of 1's. 10
9. Differentiate between NP-Complete and NP-Hard Problems and also discuss about vertex cover problem and Hamiltonian path problem with suitable examples. 10

10. Write short notes on *any two* of the following : **2x5=10**

- (a) Hypothesis of Church
  - (b) Undecidability and Rice's theorem
  - (c) Recursive and recursively enumerable languages.
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