

**B.Tech. IN ELECTRONICS AND  
COMMUNICATION ENGINEERING  
(BTECVI)**

**Term-End Examination**

**June, 2011**

**BIEL-007 : SIGNALS AND SYSTEMS**

*Time : 3 hours*

*Maximum Marks : 70*

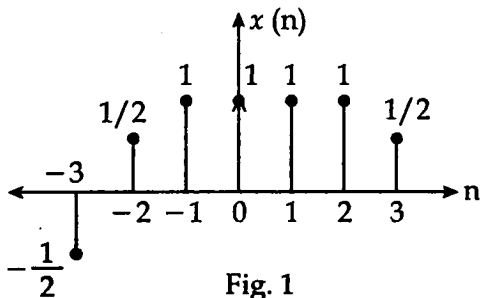
*Note : Attempt any seven questions.*

*All questions carry equal marks.*

*Use of calculator is allowed.*

1. A discrete time signal is as shown in figure 1 10  
sketch the following :

- (a)  $x(n-3)$
- (b)  $x(3-n)$
- (c)  $x(2n)$
- (d)  $x(n)u(3-n)$
- (e)  $x[(n-1)^2]$



2. Write the steps to find the convolution sum of two sequences and also find the convolution of following sequences. 10

$$x(n) = 1 ; n = -2, 0, 1$$

$$= 2 ; n = -1$$

$$= 0 \text{ else where}$$

$$h(n) = \delta(n) - \delta(n-1) + \delta(n-2) - \delta(n-3)$$

3. (a) Determine whether or not each of the following signals is periodic. If a signal is periodic, specify its fundamental period. 5

(i)  $x(n) = e^{j6\pi n}$

(ii)  $x(n) = e^{j\frac{3}{5}(n + \frac{1}{2})}$

(iii)  $x(n) = \cos\left(\frac{2\pi}{3}\right)n$

(iv)  $x(n) = \cos\frac{\pi}{3}n + \cos\frac{3\pi}{4}n$

- (b) Determine if the system described by the following input - output equations is linear or nonlinear. 5

(i)  $y(n) = x^2(n)$       (ii)  $y(n) = nx(n)$

4. Figure 2 shows a periodic square wave signal. 10  
Obtain its fourier series representation.

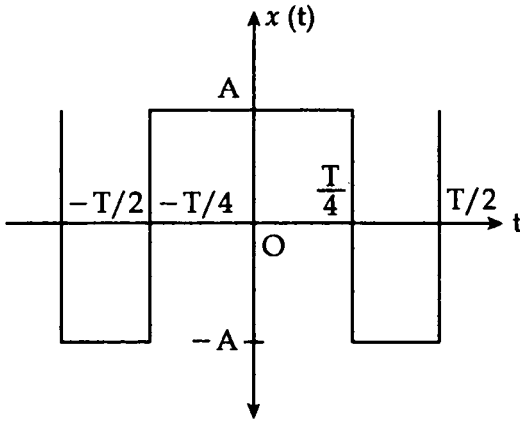


Fig. 2

5. Consider an arbitrary signal  $x(n)$  with fourier 10  
transform  $X(e^{j\omega})$ . Express the fourier transform  
of the following signals in terms of  $X(e^{j\omega})$ .

(a)  $y(n) = x(2n)$

(b) 
$$y(n) = \begin{cases} x(n/2) & n, \text{ even} \\ 0 & n, \text{ odd} \end{cases}$$

6. Find the fourier transform of the following : 10

(a) 
$$x(t) = \begin{cases} \frac{t+b}{b-a} & -b < t < -a \\ 1 & -a < t < b \\ \frac{t-b}{b-a} & a < t < b \end{cases}$$

$$(b) \quad x(n) = \left(\frac{1}{2}\right)^{n-1} \cdot u(n-1)$$

7. Use convolution to find  $x(n)$  if  $X(z)$  is given by **10**

$$X(z) = \frac{1}{\left(1 - \frac{1}{2}z^{-1}\right)\left(1 + \frac{1}{4}z^{-1}\right)}$$

8. Find the  $z$ -transform and ROC (Region of convergence) of the following sequences :- **10**

$$(a) \quad x(n) = \left(-\frac{1}{3}\right)^n u(n) - \left(\frac{1}{2}\right)^n \cdot u(-n-1)$$

$$(b) \quad x(n) = -b^n u(-n-1)$$

9. Determine the impulse response of the system **10**  
described by difference equation  
 $y(n) = y(n-1) - 0.5y(n-2) + x(n) + x(n-1)$ . Plot  
the pole zero pattern.

10. Write short notes on *any two* : **5x2=10**

- (a) Region of convergence (ROC).
- (b) Classification of signals.
- (c) Properties of Fourier Transform.