## ADCA / MCA (II Year)

Term-End Examination

## June, 2011

CS-08 : NUMERICAL AND STATISTICAL COMPUTING
Time : 3 hours
Maximum Marks : 75
Note: (i) Use of calculator is allowed.
(ii) Question number 1 is compulsory. Answer any three questions from the rest.

1. (a) What is the final value of $B$ in the following programme?
$10 \times 3=30$
$B=5.65$
$B=(B+0.09)^{*} 20$
$\mathrm{J}=\mathrm{B}$
$\mathrm{B}=\mathrm{J}$
$B=B / 10.0$
Further, if the value of $B$ were taken as 5.45 instead of 5.65 at the beginning of the above program, what would be the final value?
(b) What is the value of I calculating in the following arithmetic statements ?
(i)

$$
\begin{array}{ll}
\text { (i) } & \mathrm{I}=\mathrm{J} * 2 / 4+\mathrm{K} / 3+8-\mathrm{J} * * 3 / 8 \\
& (\mathrm{~J}=2, \mathrm{k}=6) \\
\text { (ii) } \quad \mathrm{M}=\mathrm{M}+\mathrm{N}^{*} 10 \\
\mathrm{I}=\mathrm{M} \quad(\mathrm{M}=2, \mathrm{~N}=-6)
\end{array}
$$

(iii) $\quad \mathrm{A}=\mathrm{SQRT}(\mathrm{Z} * \mathrm{~T})+\mathrm{X} * * 2$

$$
\mathrm{I}=\mathrm{A}
$$

$$
(\mathrm{Z}=12.0, \mathrm{~T}=3.0, \mathrm{X}=-4.0)
$$

(c) Write a FORTRAN 90 statement for each of the following :
(i) $\mathrm{p}=\frac{\mathrm{s}^{3}-\mathrm{t}^{3}}{\mathrm{t}+\mathrm{q}^{2}+\mathrm{e}^{x}}+\frac{\mathrm{rt}{ }^{9}}{9 s}$
(ii) $y=4 s^{2}+9 \mathrm{~s}+6+\sqrt{(\mathrm{ac})^{\mathrm{p}}}$
(iii) $v=u+a t$
(d) What is the value of $x$, if the mean of $3,4, x$, 7 , and 10 is 6 ?
(e) Given the following formula

$$
\mathrm{FDD}=\frac{1}{\mathrm{e}^{\mathrm{U}}-1}
$$

Write a FORTRAN 90 programme that will prepare a table of this function for $U$ varying from 1.0 to 10.0 in steps of 0.05 ,
(f) Write a FORTRAN 90 program that computes the value of $R, R$ is given by the relation $\frac{1}{R}=\frac{1}{R_{1}}+\frac{1}{R_{2}}, R, R_{1}, R_{2}$ are real numbers in same units.
(g) Find the line of regression of $y$ on $x$ :

| $x:$ | 1 | 2 | 3 | 4 | 5 | 8 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y:$ | 9 | 8 | 10 | 12 | 14 | 16 | 15 |

(h) The measurement (in mm) of the diameters of the heads of 107 screws gave the following frequency distribution.

| Diameter | $33-35$ | $36-38$ | $39-41$ | $42-44$ | $45-47$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 17 | 19 | 23 | 21 | 27 |

(i) A box A contains 2 white and 4 black balls. Another box $B$ contains 5 white and 7 black balls. A ball is transferred from the box A to the box $B$. Then a ball is drawn from the box $B$. Find the probability that it is white.
(j) What value will be stored in location $K$ at the end of the following sequence? Justify your answer.

$$
\begin{array}{lll}
\text { DO } & 100 & \mathrm{~J}=1,5 \\
\mathrm{~K}=5 & \\
\text { DO } & 100 & \mathrm{~N}=1,10
\end{array}
$$

$100 \mathrm{~K}=\mathrm{K}+\mathrm{N}$
PRINT *, K.
2. (a) In the following frequency distribution, the frequency of the class - interval $(40-50)$ is missing. It is known that the mean of the distribution is 52 . Find the missing frequency.
$3 \times 5=15$

| Class <br> Interval | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 5 | 3 | 4 | $?$ | 2 | 6 | 13 |

(b) The probability density function of a variable X is

| $X$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $P(X)$ | $K$ | 3 K | 5 K | 7 K | 9 K | 11 K | 13 K |

(i) Find $\mathrm{P}(\mathrm{X}<4), \mathrm{P}(\mathrm{X} \geq 5), \mathrm{P}(3<\mathrm{X} \leq 6)$
(ii) What will be the minimum value of $K$ so that $P(X \leq 2) \geq 3$ ?
(c) Write short note on Moving Average Method.
3. (a) Write a FORTRAN 90 programme that read the radius and calculate the surface area and volume of a sphere. $3 \times 5=15$
(Given Area $=4 \pi r^{2} ;$ Volume $\left.=\frac{4}{3} \pi r^{3}\right)$
(b) Explain the following :
(i) INTEGER B(60, 60)
(ii) LOGICAL MARKS (120)
(iii) REAL SALES $(20,25,5)$
(iv) REAL $\mathrm{B}(50,50)$
(v) CHARACTER * $20 \mathrm{C}(10), \mathrm{M}(60)$
(c) In an entrance test that is graded on the basis of two examination, the probability of a randomly chosen student passing the first examination is 0.8 and the probability of passing the second examination is 0.7 . The probability of passing at least one of them is 0.95 . What is the probability of passing both ?
4. (a) The data about annual production of an Indian state, is given below :

| Commodity | Wheat | Sugar | Rice | Maize | Gram |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Annual Production <br> (in tonnes) | 2750 | 2500 | 1500 | 1000 | 1250 |

Draw a pie chart to represent the above data.
(b) Given the statement :

DIMENSION A(50), B(30, 30), C(40)
Identify errors, if any, in the following FORTRAN statements.
(i) $\mathrm{Z}=\mathrm{A}(5.0)+\mathrm{B}(30.0) / 7.5$
(ii) $\mathrm{B}(1,1)=\mathrm{A} / \mathrm{C}$ * $\mathrm{A}(4) / \mathrm{B}(2,2)$
(iii) $\mathrm{DO} 66, \quad \mathrm{I}=1, \mathrm{M}$,
(iv) $\mathrm{DO} .8, \quad \mathrm{I}=\mathrm{I}, 3$
(v) $\mathrm{DO} 44 \quad \mathrm{~K}=1, \mathrm{M}+2, \mathrm{~N}$
(c) Find the errors in each of the following statements, Give reasons also
(i) The probability that it will rain tomorrow is 0.40 , and the probability that it will not rain tomorrow is 0.52 .
(ii) On a single draw from a deck of playing cards, the probability of selecting a heart is $1 / 4$, the probability
of selecting a black card is $1 / 2$ and the probability of selecting a heart and a black card is $1 / 8$.
5. (a) The two regression equations of the variables

$$
\begin{aligned}
& x \text { and } y \text { are } \\
& \qquad \begin{array}{l}
x=19.13-0.87 y, \text { and } \\
y=11.64-0.50 x
\end{array}
\end{aligned}
$$

$$
3 \times 5=15
$$

Find
(i) mean of $x$ 's
(ii) mean of $y^{\prime} \mathrm{s}$, and
(iii) the correlation coefficient between $x$ and $y$.
(b) Two one-dimensional arrays $X$ and $Y$ have 50 elements each. Write a FORTRAN program to compute and print the quantities,

$$
\begin{aligned}
& \mathrm{P}=\sum_{K=1}^{50}\left(x_{\mathrm{k}}+y_{\mathrm{k}}\right)^{2} \\
& \mathrm{R}=\sum_{\mathrm{K}=1}^{50}\left|x_{\mathrm{k}}-y_{\mathrm{k}}\right|
\end{aligned}
$$

(c) An article manufactured by a company consists of two parts A and B. In the process of manufacture of part A, 9 out of 100 are likely to be defective. Similarly, 5 out of 100 are likely to be defective in the manufacture of part $B$. Calculate the probability that the assembled article will not be defective (assuming that the events of finding the part $A$ non - defective and that of $B$ are independent)
6. (a) Find the correlation coefficient between $x$ and $y$ from the given data :

| $x:$ | 78 | 89 | 97 | 69 | 59 | 79 | 68 | 57 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y:$ | 125 | 137 | 156 | 112 | 107 | 138 | 123 | 108 |

(b) Write a FORTRAN 90 statement for each of the following :
(i) $\mathrm{EOQ}=\sqrt{\frac{2 \mathrm{DC}}{\mathrm{C}_{\mathrm{c}}}}{ }_{\mathrm{c}} \mathrm{C}_{3}$
(ii) $\mathrm{EOQ}=\sqrt{\frac{2 \mathrm{DC}_{\mathrm{o}}}{\mathrm{C}_{\mathrm{c}}}\left(\frac{\mathrm{C}_{\mathrm{c}}+\mathrm{C}_{\mathrm{s}}}{\mathrm{C}_{\mathrm{s}}}\right)}$
(iii) $\mathrm{TC}=\sqrt{2 \mathrm{DC} \mathrm{o}_{\mathrm{C}}\left(1-\frac{\mathrm{C}}{\mathrm{P}}\right)}$
(iv) $\quad R=X^{2 / 3} Y^{3 / 7}+\sqrt{(X+Y) Z}+\left|X^{2}+Y^{2}\right|$
(v) $Z=\sqrt{R^{2}+\left(\omega L-\frac{1}{\omega C}\right)^{2}}$
(c) Write short note on limb relative method.

