

**BACHELOR IN COMPUTER
APPLICATIONS**

Term-End Examination

June, 2010

17462

CS-73 : THEORY OF COMPUTER SCIENCE

Time : 3 hours

Maximum Marks : 75

Note : Question No. 1 is compulsory. Attempt any three questions from the rest.

1. (a) Explain *any five* of the following concept, 20
each with one suitable example :
- (i) Regular language
 - (ii) Finite automata
 - (iii) Context - free grammar
 - (iv) Pushdown automata
 - (v) Universal Turing Machine
 - (vi) NP - hard problem
 - (vii) Undecidable problem
- (b) (i) Construct an NFA accepting the 10
language
 $L = \{ 001, 100 \}$

(ii) Show that the language

$$L = \{a^{n^2} \mid n \geq 1\}$$

is not context free.

2. (a) For the following regular expression, 7
construct equivalent finite automata :

$$b^*a + a^*b.$$

- (b) Show that the following language L is not 8
regular :

$$L = \{a^p \mid p \text{ is a prime}\}.$$

3. (a) Tell which of the following types of 6
languages are closed under :

(i) Complementation

(ii) Intersection

(iii) Union :

(A) Regular languages

(B) Context - free languages

(C) Unrestricted languages

- (b) Show that the language : 9

$$L = \{a^n b^n c^n \mid n \geq 1\}$$

is not a context - free language.

4. (a) Give recursive definition of $\sum_{i=1}^n i$, the sum of first n natural numbers. 3

(b) Explain what is a partial function and further, why we need a partial function? 7

(c) Tell whether the square - root function 5

$$\text{SQRT} : \mathbb{N} \rightarrow \mathbb{N},$$

where \mathbb{N} denotes the set of natural numbers, is a partial function or not. Further, justify your answer.

5. (a) For the function defined as : 5

$$f(x) = 4x^5 + 7x + 11,$$

show that $f(x) = O(x^5)$,

where O denotes big oh

(b) Mention any five undecidable problems discussing each briefly. 5

(c) Name five NP-complete problems. 5