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B. Tech. IN ELECTRONICS AND COMMUNICATION ENGINEERING

Term-End Examination

December, 2011

BIEL-010 : DIGITAL SIGNAL PROCESSING

Time : 3 hours

Maximum Marks : 70

Note : Answer *any seven* questions. Each question carries *ten* marks. Use of scientific calculator is permitted.

1. What do you understand by DFT ? Prove that 3+7
the Inverse Discrete Fourier transform is given by

$$x[n] = \frac{1}{N} \sum_{k=0}^{N-1} x[k] W_N^{-kn}, 0 \leq n \leq N-1$$

2. Consider the signal $x(n) = a^n u(n)$, $0 < a < 1$. 10

The spectrum of this signal is sampled at frequencies $W_k = 2\pi k/N$, $k=0, 1, \dots, N-1$.

Determine the reconstructed spectra for $a=0.8$, when $N=5$ and $N=50$.

3. Explain the role of FFT Algorithms for 5+5
- Efficient computation of DFT of two real sequences.
 - Linear Filtering and correlation.

4. Explain circular convolution for the sequences $x_1(n)$ and $x_2(n)$ 3+7

By means of DFT and IDFT, determine the sequence $x_3(n)$ corresponding to the circular convolution of the sequences $x_1(n)$ and $x_2(n)$, where :

$$x_1(n) = \{2, 1, 2, 1\}$$

↑

$$x_2(n) = \{1, 2, 3, 4\}$$

↑

5. Explain the design of FIR filters using Rectangular Window. Write the relevant expressions and explain Gibbs phenomenon. 10
6. Determine the order of a type - I low pass chebyshev filter that has a 1 db ripple in the passband, a cut - off frequency $\Omega_p = 1000\pi$, a stopband frequency of 2000π and an attenuation of 40 db or more for $\Omega \geq \Omega_s$. Also Find its poles. 10
7. Explain the characteristics of a chebyshev filter. Draw its characteristics and define its types. 10
8. Explain an FIR filter design method using Frequency Sampling Technique. 10

9. Explain the following properties with respect to a Discrete Fourier Transform 10

- (a) Time reversal of a sequence
- (b) Circular Time Shift of a sequence
- (c) Circular Frequency Shift

10. Write short notes on *any two*.

2x5=10

- (a) Chirp Z Algorithm
 - (b) Radix - 2 FFT Algorithm
 - (c) Matched Z transform
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