M.Sc. (MATHEMATICS WITH APPLICATIONS IN COMPUTER SCIENCE)

M.Sc. (MACS)

Term-End Practical Examination

June, 2015

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MMT-007(P): DIFFERENTIAL EQUATIONS AND NUMERICAL SOLUTIONS

Time: $1\frac{1}{2}$ hours

Maximum Marks: 40

Note: (i) There are two questions in this paper totalling 30 marks.

- (ii) Answer both the questions.
- (iii) Remaining 10 marks are for the viva-voce.
- 1. Write a program in 'C' language to solve the boundary value problem

$$y'' - 3y' + 2y = 0$$
, $0 < x < 1$
 $2y(0) - y'(0) = 1$, $y(1) + y'(1) = 2e + 3e^2$

using the shooting method. Use the Taylor series method of order 2 with h=0.25 to solve the resulting initial value problem.

2. Write a program in 'C' language to find the solution of $\nabla^2 u = x^2 + y^2$ in R, subject to the given R and boundary conditions using the five-point difference formula

R: Square $0 \le x \le 1$, $0 \le y \le 1$

$$u(x, y) = \frac{x^4 + y^4}{12}$$
 on $x = 1, y = 0, y = 1$

$$12u + \frac{\partial u}{\partial x} = x^4 + y^4 + \frac{1}{3}x^3 \text{ on } x = 0.$$

Use central difference approximation in the boundary conditions and take the step length $h=\frac{1}{2}$.