# BACHELOR OF COMPUTER APPLICATIONS (BCA) <br> (Revised) 

## Term-End Examination

June, 2023

## BCS-042 : INTRODUCTION TO ALGORITHM DESIGN

Time : 2 Hours
Maximum Marks : 50
Note: (i) Question No. 1 is compulsory.
(ii) Answer any three questions from the rest.

1. (a) What is complexity of algorithm ? Explain space complexity and time complexity of algorithms with the help of example. 5
(b) Write linear search algorithm and do analysis of this algorithm for best case and worst case.
(c) Using mathematical induction method, show that for all positive integers $n$ :

$$
1^{2}+2^{2}+3^{2}+\ldots \ldots \ldots+n^{2}=\frac{n(n+1)(2 n+1)}{6}
$$

(d) What is Adjacency matrix ? Write adjacency matrix for the following graph : 5

2. (a) Write Depth-First Search (DFS) algorithm. Also traverse the following graph using DFS from node A .

(b) Solve the following recurrence relation using recurrence tree method :

$$
\mathrm{T}(n)=4 \mathrm{~T}\left(\frac{n}{2}\right)+n
$$

3. (a) Write Kruskal's algorithm for finding Minimum Cost Spanning Tree (MCST). Find MCST of the following graph using Kruskal's algorithm.

(b) Explain use of Big oh (O) notation in the analysis of algorithms with example. 2
4. (a) Find the optimal solution to the knapsack (fractional) problem for $n=5$ and $m=10$, where $n$ is the number of objects and $m$ is the capacity of the knapsack.
P. T. O.

Profit and weight of each object are given below :
$\left(\mathrm{P}_{1}, \mathrm{P}_{2}, \mathrm{P}_{3}, \mathrm{P}_{4}, \mathrm{P}_{5}\right)=(10,30,35,20,40)$
$\left(\mathrm{W}_{1}, \mathrm{~W}_{2}, \mathrm{~W}_{3}, \mathrm{~W}_{4}, \mathrm{~W}_{5}\right)=(3,5,2,6,11)$
(b) In context of algorithm study, explain the following with the help of an example of each :

4
(i) Upper Bound
(ii) Backtracking
5. (a) Sort the following list using Bubble sort algorithm. Show the steps of sorting : 6 $30,8,7,14,20,28,10,6$
(b) Write algorithm for adding two matrices of order $m \times n$ and find its time complexity. 4

