

**Ph.D. IN STATISTICS
(PHDSTAT)**

Term-End Examination

June, 2018

00175

RST-004 : ADVANCES IN STATISTICS

Time : 3 hours

Maximum Marks : 100

Note : Question no. 1 is compulsory. Attempt any four questions from questions no. 2 to 7. Non-programmable scientific calculator is allowed. Symbols have their usual meanings.

1. (a) State whether the following statements are *True* or *False*. Give reasons in support of your answers : 4×2=8

- (i) The form of Entropy Loss Function is

$$L(\Delta) \propto \Delta^{p+1} - \log \Delta^p - 1$$

where $\Delta = \hat{\theta}/\theta$.

- (ii) If $X \sim \exp(\theta)$ and prior distribution of θ is Gamma (α, β) distribution, then posterior distribution of θ is Gamma

$$(n + \alpha, \sum_{i=1}^n x_i + \beta) \text{ distribution.}$$

- (iii) In regression analysis, if $SS_{\text{Reg}} = 2.82$ and $SS_{\text{Res}} = 4.26$, then coefficient of determination is 0.398.
- (iv) For testing the significance of a multiple regression model, t-test is used.
- (b) Differentiate between the following, with suitable examples : 3×4=12
- (i) Forward and Backward selection methods
- (ii) Residual and Normal probability plots
- (iii) Linear and 0 – 1 loss functions
2. (a) Define prior and posterior distributions in Bayesian analysis. 5
- (b) Let X_1 and X_2 be random samples drawn from $N(\theta, 1)$. If prior distribution of θ is $N(\mu, 1)$, then obtain 10+5
- (i) Posterior distribution of θ .
- (ii) Bayes estimator of θ under precautionary loss function.
3. (a) Explain loss function. Define 8
- (i) Squared error loss function
- (ii) Linear exponential loss function
- (b) Let X_1, X_2, \dots, X_n be a random sample from $\exp(\theta)$ distribution and prior distribution of θ be Gamma (α, β) distribution. Obtain Bayes estimate of θ under
- (i) Squared error loss function
- (ii) Asymmetric loss function 12

4. The fuel consumption and the average speed of a car were recorded from 10 trips of the same distance covered under similar road conditions using same car. The data are given below :

Trip	Petrol Consumption (in litres)	Speed (km/hr)
1	14	50
2	10	40
3	15	45
4	16	55
5	11	35
6	16	60
7	12	55
8	14	50
9	12	40
10	10	30

- (a) Fit a regression model.
- (b) Test whether speed has any significant effect on petrol consumption at 5% level of significance.
- (c) Find 95% confidence interval for the slope.

It is given that

10+6+4

$$t_{(9),0.05} = 1.833, t_{(9),0.025} = 2.262,$$

$$t_{(8),0.05} = 1.860, t_{(8),0.025} = 2.306.$$

5. Describe various assumptions in regression analysis. 20
6. (a) Write any five properties of regression coefficients. 10
- (b) Describe Jeffrey's Prior. Let X_1, X_2, \dots, X_n be a random sample from exponential distribution with mean $1/\theta$. Construct Jeffrey's Prior. 10
7. Write detailed notes on any *two* of the following : 10+10
- (a) Residual Analysis
- (b) Use of ANOVA in Regression Analysis
- (c) Bayes Theorem
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