## POST GRADUATE DIPLOMA IN APPLIED STATISTICS (PGDAST)

Term-End Examination
00.385

## MSTL-002/S2 : INDUSTRIAL STATISTICS LAB SET-2

Time : 3 Hours
Maximum Marks : 50
Note: (i) Attempt any two questions.
(ii) Solve the questions in Microsoft Excel.
(iii) Use of Formulae and Statistical Tables Booklet for PGDAST is allowed.
(iv) Mention necessary steps, hypotheses, interpretations, etc.

1. (a) The manager of a local bank wants to study waiting times of customers for better service during the lunch hour. A sub-group of four customers is selected (one at each 15 minute interval during the lunch hour) and the time (in minutes) is measured from the point each customer enters the line to when he or she reaches the teller window. The results over a four-week period are as follows :

| Day | Time (in minutes) |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 1 | $7 \cdot 2$ | $8 \cdot 4$ | 7.9 | 4.9 |
| 2 | $5 \cdot 6$ | $8 \cdot 0$ | $3 \cdot 3$ | $4 \cdot 2$ |
| 3 | $5 \cdot 5$ | $7 \cdot 3$ | $3 \cdot 2$ | 6.0 |
| 4 | $4 \cdot 4$ | 8.0 | $5 \cdot 4$ | $7 \cdot 4$ |
| 5 | $9 \cdot 7$ | $4 \cdot 6$ | 4.8 | $5 \cdot 8$ |
| 6 | $8 \cdot 3$ | $8 \cdot 9$ | $9 \cdot 1$ | $6 \cdot 2$ |
| 7 | $4 \cdot 7$ | $6 \cdot 6$ | $5 \cdot 3$ | $5 \cdot 8$ |
| 8 | $8 \cdot 8$ | $5 \cdot 5$ | $8 \cdot 4$ | 6.9 |
| 9 | $5 \cdot 7$ | $4 \cdot 7$ | $4 \cdot 1$ | $4 \cdot 6$ |
| 10 | $3 \cdot 7$ | $14 \cdot 0$ | 3.0 | $5 \cdot 2$ |
| 11 | $2 \cdot 6$ | $3 \cdot 9$ | $5 \cdot 2$ | $4 \cdot 8$ |
| 12 | $4 \cdot 6$ | $2 \cdot 7$ | 6.3 | $3 \cdot 4$ |
| 13 | 4.9 | $6 \cdot 2$ | $7 \cdot 8$ | 8.7 |
| 14 | $7 \cdot 1$ | $6 \cdot 3$ | $8 \cdot 2$ | $5 \cdot 5$ |
| 15 | $7 \cdot 1$ | $5 \cdot 8$ | $6 \cdot 9$ | $17 \cdot 0$ |
| 16 | $6 \cdot 7$ | $6 \cdot 9$ | $7 \cdot 0$ | $9 \cdot 4$ |
| 17 | $5 \cdot 5$ | $6 \cdot 3$ | $3 \cdot 2$ | $4 \cdot 9$ |
| 18 | 4.9 | $5 \cdot 1$ | $3 \cdot 2$ | $7 \cdot 6$ |
| 19 | $7 \cdot 2$ | 8.0 | $4 \cdot 1$ | $5 \cdot 9$ |
| 20 | $6 \cdot 1$ | $3 \cdot 4$ | $7 \cdot 2$ | $5 \cdot 9$ |

Draw suitable control charts for process mean and process variability. Comment whether the process is under statistical control. If not, draw the revised charts.
(b) Suppose a rice shopkeeper wants to analyse his monthly sales. The data of the total quantity of rice sold (in kg ) every month for 3 years from 2015-2017 are recorded in the table given below :

| Month | Sale | Month | Sale | Month | Sale |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 396 | 13 | 689 | 25 | 848 |
| 2 | 396 | 14 | 596 | 26 | 774 |
| 3 | 450 | 15 | 540 | 27 | 694 |
| 4 | 648 | 16 | 630 | 28 | 765 |
| 5 | 764 | 17 | 879 | 29 | 1134 |
| 6 | 824 | 18 | 990 | 30 | 1224 |
| 7 | 802 | 19 | 1032 | 31 | 1210 |
| 8 | 812 | 20 | 1020 | 32 | 1237 |
| 9 | 776 | 21 | 1005 | 33 | 1248 |
| 10 | 767 | 22 | 1017 | 34 | 1217 |
| 11 | 760 | 23 | 967 | 35 | 1215 |
| 12 | 738 | 24 | 924 | 36 | 1134 |
| 1 |  |  |  |  |  |
| 1 |  |  |  |  |  |

(i) Compute 3- and 6-monthly moving averages. Plot the results along with the data.
(ii) Use the exponential smoothing coefficients of 0.5 and 0.1 to compute the exponentially smoothed series.
2. A researcher wants to develop a regression model to predict the market price (in lakh rupees) of a house by two variables, viz. Total area (in square feet) and Age of the house (in years). The data are given below :

| Market price | Total area | Age of house |
| :---: | :---: | :---: |
| $40 \cdot 0$ | 1605 | 15 |
| 42.0 | 2489 | 25 |
| $45 \cdot 2$ | 1552 | 10 |
| $50 \cdot 2$ | 2404 | 12 |
| $43 \cdot 9$ | 1884 | 15 |
| $53 \cdot 5$ | 1558 | 10 |
| $44 \cdot 9$ | 1748 | 6 |
| 58.0 | 3105 | 8 |
| $40 \cdot 7$ | 1682 | 15 |
| $42 \cdot 0$ | 2470 | 15 |
| 59.5 | 1820 | 2 |
| $63 \cdot 9$ | 2143 | 6 |
| 59.7 | 2121 | 10 |
| 64.5 | 2485 | 9 |
| $60 \cdot 2$ | 2300 | 15 |
| 89.5 | 2714 | 4 |
| 82.5 | 2463 | 5 |
| 101.0 | 3076 | 7 |
| $84 \cdot 9$ | 3048 | 3 |
| 108.0 | 3264 | 6 |
| $95 \cdot 0$ | 3069 | 5 |
| 88.5 | 4765 | 20 |
| $110 \cdot 0$ | 4540 | 8 |

(i) Prepare a scatter matrix to get a rough idea about the relationship among the variables.
(ii) Develop a multiple linear regression model using the matrix approach.
(iii) Test the significance of the fitted model at $5 \%$ level of significance and construct the $95 \%$ confidence interval of the regression parameters.
(iv) Also check the linearity and normality assumptions for the fitted model.
$5+8+6+6$
3. (a) The data given below represents the profit (in million rupees) of a company on a monthly basis from January 2014 to December 2017 :

| Month |  | Year |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  |  | 2015 | 2016 | 2017 |  |
| January | 2.87 | 2.86 | 2.95 | 3.19 |  |
| February | 2.84 | 2.90 | 2.96 | 3.28 |  |
| March | 3.04 | 3.09 | 3.13 | 3.33 |  |
| April | 3.50 | 3.28 | 3.30 | 3.43 |  |
| May | 3.59 | 3.53 | 3.46 | 3.60 |  |
| June | 3.92 | 3.97 | 4.05 | 3.89 |  |
| July | 3.97 | 4.06 | 4.16 | 4.02 |  |
| August | 3.76 | 4.03 | 3.82 | 3.85 |  |
| September | 3.44 | 3.65 | 3.43 | 3.56 |  |
| October | 3.47 | 3.72 | 3.52 | 3.55 |  |
| November | 3.26 | 3.36 | 3.42 | 3.22 |  |
| December | 2.94 | 3.16 | 3.20 | 2.95 |  |

(i) Calculate the seasonal indices using ratio to trend method.
(ii) Obtain the deseasonalised values.
(iii) Plot original data and deseasonalised data.
(b) The table given below indicates the number of medical sponges produced daily and the number that are non-conforming for a period of 32 days :

| Day | Sponges produced | Non-conforming sponges | Day | Sponges produced | Non-conforming sponges |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 690 | 21 | 17 | 575 | 20 |
| 2 | 580 | 22 | 18 | 610 | 16 |
| 3 | 685 | 20 | 19 | 596 | 15 |
| 4 | 595 | 21 | 20 | 630 | 24 |
| 5 | 665 | 23 | 21 | 625 | 25 |
| 6 | 596 | 19 | 22 | 615 | 21 |
| 7 | 600 | 18 | 23 | 575 | 23 |
| 8 | 620 | 24 | 24 | 572 | 20 |
| 9 | 610 | 20 | 25 | 645 | 24 |
| 10 | 595 | 22 | 26 | 651 | 39 |
| 11 | 645 | 19 | 27 | 660 | 21 |
| 12 | 675 | 23 | 28 | 685 | 19 |
| 13 | 670 | 22 | 29 | 671 | 17 |
| 14 | 590 | 26 | 30 | 660 | 22 |
| 15 | 585 | 17 | 31 | 595 | 24 |
| 16 | 560 | 16 | 32 | 600 | 16 |

Construct a suitable control chart and state whether the process is under statistical control. If not, draw the revised chart.

