

**B.Tech. – VIEP – ELECTRICAL ENGINEERING
(BTELVI)**

Term-End Examination

00413

June, 2018

BIEEE-002 : DIGITAL CONTROL SYSTEM

Time : 3 hours

Maximum Marks : 70

Note : Attempt any seven questions. All questions carry equal marks. Use of scientific calculator is allowed.

1. Give the block-diagram representation of the state-model of a discrete-time multivariable LTI system. Also find the solution of the state equation of a discrete-time LTI system by using z-transform approach. 10

2. Consider the system described by the equations

$$x_1(k + 1) = 2x_1(k) + 0.5 x_2(k) - 5$$

$$x_2(k + 1) = 0.8 x_2(k) + 2$$

Investigate the stability of the equilibrium state using Lyapunov equation. 10

3. Obtain the transfer function description for the following system : 10

$$\begin{bmatrix} x_1(k+1) \\ x_2(k+1) \end{bmatrix} = \begin{bmatrix} 2 & -5 \\ \frac{1}{2} & -1 \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} u(k)$$

$$y(k) = 2x_1(k)$$

4. Discuss the Jury's stability criterion. Also investigate the stability of the discrete-time system described by the characteristic polynomial 10

$$P(z) = 3z^4 + 6z^3 + (1 + 4z) + 10z^2$$

5. Solve for $y(k)$ when

$$y(k) = r(k) - r(k-1) - y(k-1); k \geq 0$$

where,

$$r(k) = \begin{cases} 1 & ; \quad k \text{ even} \\ 0 & ; \quad k \text{ odd} \end{cases}$$

$$\text{and } y(-1) = r(-1) = 0 \quad 10$$

6. Find $y(z)$ for the sampled-data closed-loop system of Figure 1. 10

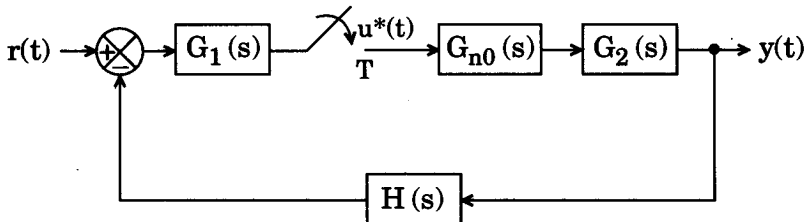


Figure 1

7. A continuous-time plant described by the equation

$$\dot{y} = -y + u + w$$

is to be controlled by a digital computer. y is the output, u is the input and w is the disturbance signal. Sampling interval $T = 1$ sec. Obtain a discrete-time state-variable model of the plant. 10

8. How does the sampling period influence the controllability and observability of the sampled system? 10

9. Write short notes on any *two* of the following: $2 \times 5 = 10$

- (a) Stability Improvement by State-Feedback
 - (b) Optimal Digital Control
 - (c) Bilinear Transformation
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