

MCA (Revised)

Term-End Examination

June, 2018

01035

MCS-033 : ADVANCED DISCRETE MATHEMATICS

Time : 2 hours

Maximum Marks : 50

Note : Question no. 1 is compulsory. Attempt any three questions from the rest.

1. (a) Write the recurrence relation of Tower of Hanoi problem and explain the formulation. 4
- (b) A person invested ₹ 10,000 @ 12% interest compounded annually. How much will he get at the end of 15 years ? (Solve using recurrence relation only) 4
- (c) Explain generating function. What type of problems can be solved using generating function for recurrence relation ? 4

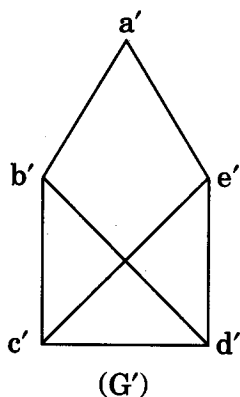
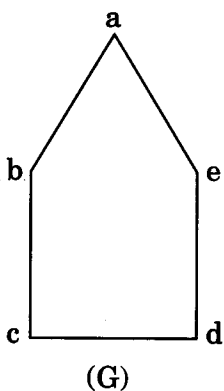
(d) Is there a simple graph corresponding to the following degree sequence : 4

(i) (1, 1, 2, 3)

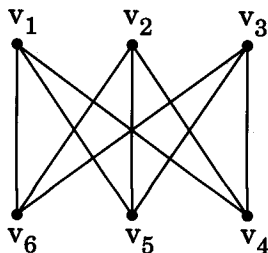
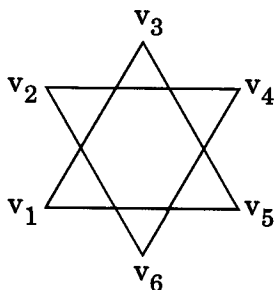
(ii) (2, 2, 4, 6)

(e) For what value of n is the graph of K_n Eulerian ? 4

2. (a) Find whether the following pair of graphs are isomorphic or not. 5



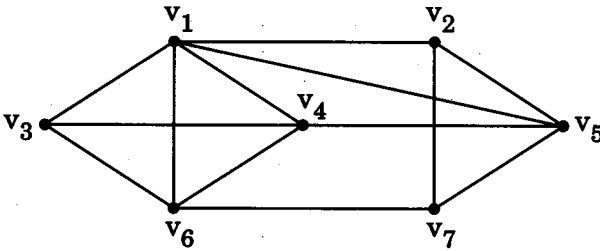
(b) The following graph contains no Euler circuit. Give reasons. 5



3. (a) If G is a connected simple graph with $(h \geq 3)$ vertices and e edges then 5

$$e \leq 3n - 6$$

- (b) Consider the graph G . Use suitable graph colouring algorithm to colour G and find $\chi(G)$. 5



4. (a) Solve

$$a_{n+2} - 5a_{n+1} + 6a_n = 2$$

with initial condition $a_0 = 1, a_1 = -1$. 5

- (b) Determine the generating function of the following sequence : 5

$$a_r = \begin{cases} 2^r & \text{if } r \text{ is even} \\ -2^r & \text{if } r \text{ is odd} \end{cases}$$

5. (a) Determine the number of integer solutions to linear equation 5

$$x_1 + x_2 = 3 \text{ with } 0 \leq x_1 \leq 1 \text{ and } 0 \leq x_2 \leq 2.$$

- (b) Show that $a_n = -2^{n+1}$ is the solution of the non-homogeneous linear recurrence relation 5

$$a_n = 3a_{n-1} + 2^n$$
