# BACHELOR OF COMPUTER APPLICATIONS (BCA) (Revised) 

Term-End Examination

## June, 2018

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## BCS-042 : INTRODUCTION TO ALGORITHM DESIGN

Time : 2 hours
Maximum Marks : 50
Note: Question no. 1 is compulsory and carries 20 marks. Answer any three questions from the rest.

1. (a) Define O (Big-"Oh") notation. By using basic definition of $O$, show that $\left(3 x^{2}+4 x+1\right)=O\left(x^{2}\right)$.
(b) The recurrence relation for Fibonacci sequence is given by $t_{n}=t_{n-1}+t_{n-2}$, such that $t_{0}=0$ and $t_{1}=1$. Find the solution of this recurrence.
(c) Find the optimal solution to the fractional knapsack instance $\mathrm{n}=5$, $\operatorname{capacity}(\mathrm{M})=10$;

$$
\begin{align*}
& \left(p_{1}, p_{2}, \ldots, p_{5}\right)=(12,32,40,30,50) \\
& \left(w_{1}, w_{2}, \ldots, w_{5}\right)=(4,8,2,6,1) \tag{5}
\end{align*}
$$

(d) Write Adjacency list and Adjacency matrix representation for the following graph :

(e) Find time complexity of the following code :

$$
\begin{aligned}
& \text { for }(i=1 ; i<=n ; i++) \\
& \text { for }(j=1 ; j<=n ; j=j * 2) \\
& \text { Sum[i] }=\operatorname{Sum}[i]+i \times j
\end{aligned}
$$

2. (a) Differentiate between Depth-First Search (DFS) and Breadth-First Search (BFS) in terms of time and space complexity. Traverse the following graph using (i) DFS, (ii) BFS, the starting node is A.

(b) List all the steps to be used to search 30 in the following list using binary search :

$$
\begin{array}{lllllll}
6 & 8 & 10 & 12 & 30 & 32 & 35
\end{array}
$$

3. (a) Write Quick-sort algorithm and find its time complexity in worst case.

5
(b) Multiply $10265 \times 2573$ using Divide and Conquer technique. Apply Karatsuba method.
4. Write any two applications of spanning tree. Write Prim's algorithm and apply it to find the minimum cost spanning tree for the following graph :

5. (a) Write all the (3) cases of Master method for solving Recurrence. Apply Master method to solve the following recurrence :

$$
T(n)=3 T\left(\frac{n}{4}\right)+n \log n
$$

(b) Write algorithm of bubble sort.

