

**B.Tech. - VIEP - ELECTRICAL ENGINEERING
(BTELVI)**

Term-End Examination

00254

June, 2017

**BIEEE-009 : DIGITAL CONTROL SYSTEM
DESIGN**

Time : 3 hours

Maximum Marks : 70

Note : Answer any **seven** questions. All questions carry equal marks. Symbols used have their usual meanings.

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1. (a) Determine the Z-transform of a unit ramp function. 5
 - (b) Find the transfer function of a first-order hold. Sketch the output of a first-order hold. 5
 2. (a) What is the effect of sampling on the spectrum ? 5
 - (b) Determine the pulse transfer function for the system with open loop transfer function $G(s) = \frac{s+2}{s+1}$. The sampling time is $T = 0.5$ sec. 5

3. For the sampled data system shown in Figure 1, obtain the final value of $C(kT)$ for a unit step input with sampling period $T = 1$ sec. Write the expression of $C(kT)$. 10

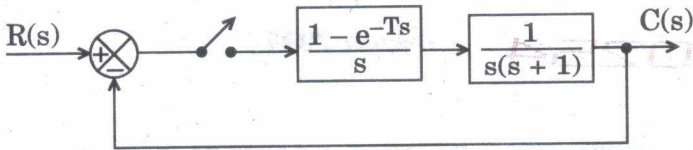


Figure 1

4. (a) Explain Jury's criterion of stability analysis. 5
- (b) Find the stability of the system, given the characteristic polynomial
- $$F(z) = 3z^4 + 7z^3 + 10z^2 + 4z + 1. \quad 5$$
5. (a) Write the merits of state-space representation. 5
- (b) Obtain a state-space representation for the difference equation
- $$c(k+2) + 0.7c(k+1) + 0.1c(k) = 2f(k+1) + f(k). \quad 5$$
6. Determine the characteristics $D(z)$ of a digital controller such that the response of the system to a unit step function will be $C(t) = 1 - e^{-0.5t}$. The transfer function for the plant is $\frac{1}{1+5s}$ and the sampling period $T = 1$ sec. 10

7. (a) State the properties of the state transition matrix. 5

(b) Given the matrix $F = \begin{bmatrix} 0 & 1 \\ -15 & -1 \end{bmatrix}$, determine $\phi(k) = F^k$ using the Z-transform method. 5

8. (a) Define the following terms : 5

(i) Stabilizability

(ii) Reachability

(b) Consider an n^{th} order SISO system

$$\dot{\mathbf{x}} = \mathbf{A}\mathbf{x} + \mathbf{b}u; \quad y = \mathbf{c}\mathbf{x}.$$

Assume the feedback of the form $u = -\mathbf{k}\mathbf{x} + r$, where r is the reference input signal. Show that the zeroes of the system are invariant under state feedback. 5

9. Write short notes on any **two** of the following : 2×5=10

(a) Multirate Discrete Data Systems

(b) Cascade Compensation using Bilinear Transformation

(c) Root Locus Plot

(d) Deadbeat Controller