POST GRADUATE DIPLOMA IN APPLIED STATISTICS (PGDAST)
Term-End Examination
June, 2016

MSTL-002/S1 : INDUSTRIAL STATISTICS LAB SET-1
Time : 3 Hours
Maximum Marks : 50
Note: (i) Attempt any two questions.
(ii) Solve the questions in Microsoft Excel.
(iii) Use of Formulae and Statistical Tables Booklet for PGDAST is allowed.
(iv) Mention necessary steps, hypothesis, interpretation, etc.
(v) Symbols have their usual meanings.

1. (a) A new process of producing ball bearings is started. For monitoring the outside diameter of the ball bearings, the quality controller takes samples of four ball bearings at 10.00 A.M., 12.00 Noon, 2.00 P.M., 4.00 P.M. and 6.00 P.M. The outside diameter (in mm ) of each selected ball bearing is measured. The results of the measurement over a 5 -day production period are as follows :

| Day | Sample Number | Time | Observations |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\mathrm{X}_{1}$ | $\mathrm{X}_{2}$ | $\mathrm{X}_{3}$ | $\mathrm{X}_{4}$ |
| Monday | 1 | 10.00 A.M. | 52 | 52 | 50 | 51 |
|  | 2 | 12.00 Noon | 50 | 53 | 52 | 53 |
|  | 3 | 2.00 P.M. | 54 | 51 | 50 | 52 |
|  | 4 | 4.00 P.M. | 62 | 65 | 60 | 62 |
|  | 5 | 6.00 P.M. | 51 | 52 | 50 | 53 |
| Tuesday | 6 | 10.00 A.M. | 50 | 52 | 51 | 50 |
|  | 7 | 12.00 Noon | 50 | 54 | 52 | 51 |
|  | 8 | 2.00 P.M. | 52 | 51 | 53 | 50 |
|  | 9 | 4.00 P.M. | 52 | 53 | 52 | 55 |
|  | 10 | 6.00 P.M. | 51 | 51 | 50 | 51 |
| Wednesday | 11 | 10.00 A.M. | 52 | 52 | 54 | 62 |
|  | 12 | 12.00 Noon | 49 | 48 | 50 | 50 |
|  | 13 | 2.00 P.M. | 52 | 53 | 54 | 49 |
|  | 14 | 4.00 P.M. | 52 | 51 | 54 | 51 |
|  | 15 | 6.00 P.M. | 51 | 51 | 52 | 52 |

P.T.O.

| Day | Sample <br> Number | Time | Observations |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\mathrm{X}_{2}$ | $\mathrm{X}_{3}$ | $\mathrm{X}_{4}$ |  |
|  | 16 |  | 50 | 50 | 51 | 52 |
|  | 17 | 12.00 Noon | 50 | 51 | 53 | 51 |
|  | 18 | 2.00 P.M. | 52 | 50 | 49 | 53 |
|  | 19 | 4.00 P.M. | 52 | 51 | 54 | 51 |
|  | 20 | 6.00 P.M. | 45 | 43 | 50 | 52 |
|  | 21 | 10.00 A.M. | 52 | 54 | 53 | 50 |
|  | 22 | 12.00 Noon | 50 | 50 | 52 | 51 |
|  | 23 | 2.00 P.M. | 54 | 52 | 50 | 52 |
|  | 24 | 4.00 P.M. | 50 | 54 | 54 | 50 |
|  | 25 | 6.00 P.M. | 51 | 51 | 50 | 52 |

(i) Which control charts should be used to control the process mean and process variability of the process of producing ball bearings?
(ii) Construct these charts and check whether the process is under statistical control or not.
(iii) Also plot the revised control charts, if necessary.
(b) An electronics firm is manufacturing computer memory chips. Statistical quality control methods are to be used to monitor the quality of the chips produced. Any chip that does not meet specifications is classified as defective. 250 chips are sampled on each of the 30 consecutive working days. The number of defective chips found each day are recorded in the following table :

| Working <br> Day | No. of <br> Defectives | Working <br> Day | No. of <br> Defectives | Working <br> Day | No. of <br> Defectives |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 12 | 11 | 20 | 21 | 15 |
| 2 | 8 | 12 | 15 | 22 | 16 |
| 3 | 18 | 13 | 11 | 23 | 7 |
| 4 | 14 | 14 | 14 | 24 | 14 |
| 5 | 9 | 15 | 7 | 25 | 12 |
| 6 | 13 | 16 | 15 | 26 | 8 |
| 7 | 10 | 17 | 12 | 27 | 14 |
| 8 | 14 | 18 | 8 | 28 | 12 |
| 9 | 8 | 19 | 22 | 29 | 8 |
| 10 | 12 | 20 | 9 | 30 | 10 |

(i) Construct the appropriate control chart and state whether the process is under statistical control or not.
(ii) Calculate the revised centre line and control limits to bring the process under statistical control. Also plot the revised control chart. 5+5
2. The number of accidents on a particular stretch of highway seems to be related to the number of vehicles and the speed at which they are travelling. A city councillor has decided to examine the data statistically so that new speed laws, that will reduce traffic accidents, may be introduced. The data for 40 randomly selected days is given in the following table :

| No. of <br> Accidents | No. of <br> Vehicles | Average Speed <br> $(\mathrm{km} / \mathrm{h})$ | No. of <br> Accidents | No. of <br> Vehicles | Average Speed <br> $(\mathrm{km} / \mathrm{h})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 2123 | 68 | 13 | 3484 | 75 |
| 6 | 2501 | 74 | 5 | 2400 | 60 |
| 12 | 2722 | 83 | 12 | 3220 | 71 |
| 3 | 2214 | 63 | 11 | 3092 | 78 |
| 17 | 2840 | 80 | 12 | 3200 | 75 |
| 8 | 2625 | 71 | 7 | 2901 | 66 |
| 12 | 2723 | 78 | 4 | 2682 | 68 |
| 4 | 2146 | 60 | 5 | 2880 | 59 |
| 8 | 2682 | 71 | 2 | 2102 | 60 |
| 14 | 3203 | 82 | 6 | 2943 | 55 |
| 10 | 3100 | 68 | 8 | 3012 | 76 |
| 11 | 2842 | 72 | 10 | 3407 | 78 |
| 12 | 3002 | 75 | 12 | 3450 | 60 |
| 20 | 3526 | 88 | 6 | 2703 | 58 |
| 6 | 2405 | 64 | 3 | 2260 | 72 |
| 7 | 3201 | 65 | 3 | 2406 | 60 |
| 2 | 2318 | 63 | 4 | 3012 | 77 |
| 10 | 2845 | 72 | 6 | 3210 | 62 |
| 8 | 3017 | 70 | 4 | 3121 | 60 |
| 11 | 3284 | 70 | 12 | 3429 | 68 |

(a) Prepare a scatter matrix to get a rough idea about the relationship among the variables.
(b) Develop a multiple linear regression model.
(c) Test the significance of the fitted regression model and individual regression coefficient at $1 \%$ level of significance.
(d) Find the $99 \%$ confidence interval of the regression parameters.
(e) Check the linearity and normality assumptions for regression analysis.
3. The following data refers to the sales of commercial vehicles at the All India level of a leading automobile company in the country during three financial years :

| Month | Year |  |  |
| :--- | :---: | :---: | :---: |
|  | 2013 | 2014 | 2015 |
| April | 724 | 1414 | 1243 |
| May | 1440 | 2117 | 1818 |
| June | 1606 | 2199 | 2880 |
| July | 1656 | 2583 | 1693 |
| August | 1549 | 2358 | 2136 |
| September | 2285 | 3677 | 3707 |
| October | 1523 | 1823 | 1931 |
| November | 1856 | 2372 | 1637 |
| December | 2135 | 2301 | 1746 |
| January | 2119 | 2761 | 2638 |
| February | 2075 | 2110 | 2655 |
| March | 3850 | 3996 | 3576 |

(a) Compute 12 -monthly moving averages and plot the graph of the moving averages with the sales data.
(b) Compute the seasonal indices for 12 months.
(c) Obtain deseasonalised values.
(d) Plot the given data along with deseasonalised values.

