

**BACHELOR OF COMPUTER APPLICATIONS
(PRE-REVISED)**

Term-End Examination

June, 2014

**CS-71 : COMPUTER ORIENTED NUMERICAL
TECHNIQUES**

Time : 3 hours

Maximum Marks : 75

Note : Question number 1 is compulsory. Attempt any three from question number 2 to 5. Calculator is allowed.

1. (a) Show that $a(b - c) \neq ab - ac$
 where $a = 0.5555 \times 10^1$, $b = 0.4545 \times 10^1$,
 $c = 0.4535 \times 10^1$ using four decimal digit
 arithmetic with rounding. **6x5=30**
- (b) Give floating point representation of
 following in two decimal digits and four
 decimal digits with rounding
 0.4861416×10^2 , 2.3748, 0.0436
- (c) Solve using Cramer's Rule
- $$x + y + z = 7$$
- $$2x + 3y + 2z = 17$$
- $$4x + 9y + z = 37$$
- (d) Perform three iteration to find cube root of
 41 using Newton-Raphson Method.

- (e) Find Lagrange Interpolating polynomial for the following :

x	2.5	3.5
$f(x)$	6	8

Also find $f(3)$?

- (f) Solve the following initial value problem using Heun's method of $O(h^2)$ where $y' = -ty^2$, $y(2) = 1$ find $y(2.1)$; $h = 0.1$.
2. (a) Find real root of the equation $f(x) = x^3 - 4x - 9 = 0$ using Bisection Method in four iterations. **3x5=15**
- (b) Solve the following system of equation by Gauss Elimination Method
- $$54x + y + z = 110$$
- $$2x + 15y + 6z = 72$$
- $$-x + 6y + 27z = 85$$
- (c) Find root of the equation $f(x) = x \log_{10} x - 1.2$ by Regular Falsi Method upto 4 decimal places.
3. (a) Perform three iteration using Jacobi Method for following system of equation **3x5=15**

$$\begin{bmatrix} -8 & 1 & 1 \\ 1 & -5 & -1 \\ 1 & 1 & -4 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 1 \\ 16 \\ 7 \end{bmatrix}$$

- (b) Evaluate $\int_0^1 \frac{dx}{1+x^2}$ by subdividing the interval (0,1) into 6 equal parts using $\frac{1}{3}$ rd Simpson's Rule.

- (c) Apply Secant method to find a root of the equation $2x^3 + 3x^2 + 3x + 1 = 0$ with initial approximations as $x_0 = -0.2$, $x_1 = -0.4$.

4. (a) Use Taylor Series Method to solve the equation **3x5=15**

$$y' = x^2 + y^2$$

for $x = 0.25$ and $x = 0.5$

given that $y(0) = 1$.

- (b) Find Newton's Backward Difference form of interpolating polynomial for the data

x	4	6	8	10
$f(x)$	19	40	79	142

Hence interpolate $f(9)$.

- (c) Evaluate $\int_0^1 \frac{dx}{1+x^2}$ by subdividing the interval $(0,1)$ into 6 equal parts using Trapezoidal Rule.

5. (a) Find y where $x = 0.1$, given that $y(0) = 1$ and $y' = x^2 + y$ with step length $h = 0.05$ using Euler Method. **3x5=15**

- (b) Given $\frac{dy}{dx} = \frac{y-x}{y+x}$, $y(0) = 1$, $h = 0.2$ find $y(0.2)$ upto 4 decimal places using Runge-Kutta Method of fourth order.

- (c) Find value of x where $y = 3$ from the following

x	4	7	10	12
y	-1	1	2	4

Using Lagrange's inverse interpolation ?