

**M.Sc. (MATHEMATICS WITH APPLICATIONS
IN COMPUTER SCIENCE)**

M.Sc. (MACS)

Term-End Examination

June, 2013

00322

**MMTE-007 : SOFT COMPUTING AND ITS
APPLICATIONS**

Time : 2 hours

Maximum Marks : 50

(Weightage : 50%)

Note : Question No. 7 is Compulsory. Attempt any four questions from Q. No. 1 to 6. Use of calculator is not allowed.

1. (a) Consider a local area network of inter connected workstations that communicate using Ethernet protocols at a maximum rate of 10 M bit/s. Traffic rates on the network can be expressed as the peak value of the total bandwidth (BW) used, and the two fuzzy variables, "Quiet" and "Congested", can be used to describe the perceived loading of the LAN. If the discrete universal set $X = \{0, 1, 2, 5, 7, 9, 10\}$ represents bandwidth usage, then the membership grades of these elements in the fuzzy sets quiet Q and congested C are given in the table and Fig.1. 10

x (BW), M bit/s	$\mu_Q(x)$	$\mu_C(x)$
0	1.0	0.0
1	1.0	0.0
2	0.8	0.0
5	0.3	0.4
7	0.1	0.6
9	0.0	0.8
10	0.0	1.0

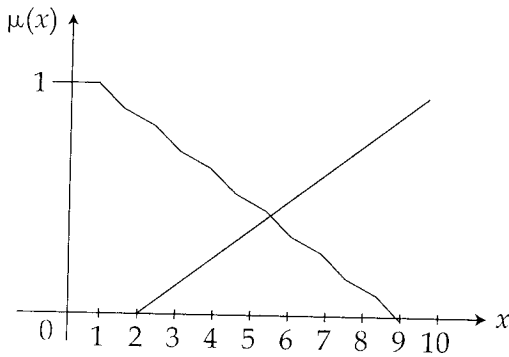
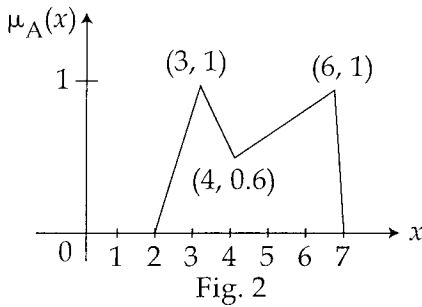


Fig. 1 : Membership functions of quiet and congested.

- (b) For these two fuzzy sets find the union, intersection, complement of Q , difference $Q - C$, and verify any one of Demorgan's law
- (i) graphically and
 - (ii) numerically.

2. (a) Given a fuzzy set A with the membership function given fig 2. 4



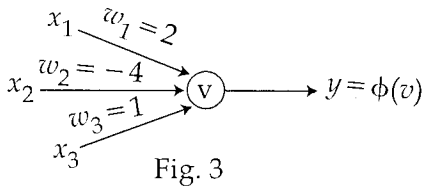
Derive $\mu_A(x)$ as a mathematical function.

- (b) Use a binary-coded Genetic algorithm (GA) 6
to minimize the function

$$f(x_1, x_2) = x_1 + x_2 - 2x_1^2 - x_2^2 + x_1, x_2, \text{ in the range of } 0 \leq x_1, x_2 \leq 5.$$

Use a random population of size $N=6$, a single point crossover with probability $P_c=1$ and neglect mutation. Assume 3 bits for each variable and thus the GA - string will be 6 - bits long. Show only one iteration by hand calculation.

3. (a) Consider the single layer perceptron given in Fig 3. 6



7. Which of the following statements are **true** or **false**. Give reasons for your answers. 10
- (a) The support of a fuzzy set A is same as the α - cut of a fuzzy set A.
 - (b) The Manhattan distance and the Minkowski distance are same for some condition.
 - (c) The input to a single input neuron is 2, its weight is 2.3 and its bias is -3 . The neuron output for Linear transfer function is -1 .
 - (d) The SOM is useful for classification.
 - (e) The length and order of the schema $S = (0^{**}11^{*}0^{**})$ are 6 and 3 respectively.
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The activation function is given by

$$\phi(v) = \begin{cases} 1; & v \geq 0 \\ 0; & v < 0 \end{cases}$$

Calculate the output y of the unit for each of the following input pattern :

Patterns	p_1	p_2	p_3	p_4
x_1	1	0	1	1
x_2	0	1	0	1
x_3	0	1	1	1

- (b) Describe the Binary Hopfield network with the help of an example. 4
4. (a) Define the following operations in Genetic algorithm with one example of each. 4
- (i) Crossover
- (ii) Mutation
- (b) Consider the ADALINE filter with three neurons in the input layer having weights $W_{11}=3$, $W_{12}=1$ and $W_{13}=-2$ and the input sequence. 6
- { - - - , 0, 0, 0, -4, 5, 0, 0, 0 - - - }
- What is the filter output ?

5. (a) If the input vectors are $I_1 = [-1, 0]^T$, and $I_2 = [0, 1]^T$, and the initial values of two weight vectors are $[0, 1]^T$ and $[\frac{2}{\sqrt{5}}, \frac{-1}{\sqrt{5}}]$ calculate the resulting weight found after training the competitive layer with the Kohonen's rule and a learning rate α of 0.4 on the input series in order I_1 , and I_2 . 8
- (b) Differentiate between bounded sum and algebraic sum of two fuzzy sets. 2
6. (a) What do you mean by a feed - forward neural network ? Using diagram, show how it differs from a recurrent neural network. 4
- (b) Consider the two parents which are participating in partially mapped cross over as shown below : 6

Parent 1 : C D | E A B I | H G F

Parent 2 : A B | C D E F | G H I

Using partially mapped crossover assuming 2nd and 6th as the crossover sites, find the children solution.