

DIPLOMA VIEP COMPUTER SCIENCE AND ENGINEERING (BTCSEVI)

Term-End Examination

June, 2013

BICS-033 : NUMERICAL METHODS AND COMPUTATION

Time : 2 hours

Maximum Marks : 70

Note : Attempt any five questions. Question No. 1 is Compulsory. Calculator is allowed.

1. (a) If a number is rounded to k decimal places, then the absolute error is : $7 \times 2 = 14$
- (i) $\frac{1}{2} 10^{k-1}$ (ii) $\frac{1}{2} 10^{-k}$
- (iii) $\frac{1}{3} 10^k$ (iv) $\frac{1}{4} 10^{-k}$
- (b) The Newton - Raphson method fails when :
- (i) $f'(x) < 0$ (ii) $f'(x) > 0$
- (iii) $f'(x) = 0$ (iv) Never fails
- (c) The relation between E , Δ and ∇ is :
- (i) $\Delta = E \cdot \nabla$ (ii) $E = \nabla - \Delta$
- (iii) $\Delta = \frac{E}{\nabla}$ (iv) None of these

- (d) Relation between E and Δ is :
- (i) $E = 1 + \Delta$ (ii) $E = 1 - \Delta$
 (iii) $E = \Delta - 1$ (iv) None of these
- (e) Interpolation is the technique of estimating the value of a function for any _____.
- (f) Any solution to a L.P.P which satisfies the non-negativity restrictions of the problem is called its _____.
- (g) Whenever Trapezoidal rule is applicable Simpson's $\frac{1}{3}$ rd rule can also be applied. (True/False).
2. (a) Find a root of the equation, $x - \cos x = 0$, using bisection method correct to 3 decimal places. 7
- (b) Using Regula-Falsi method find a root of $2x - \log x = 6$ correct to 3 decimal places. 7
3. (a) Find a root of the equation $x^3 + x^2 + x + 7 = 0$ correct to 3 decimal places by Secant method. 7
- (b) Find the positive root of $x^4 - x = 10$ correct to three decimal places using Newton - Raphson method. 7

4. (a) Solve by Gauss elimination method for the following equations : 7
 $2x + 2y + z = 12$
 $3x + 2y + 2z = 8$
 $5x + 10y - 8z = 10$
- (b) Solve by Gauss-Seidal method, for the following equations : 7
 $2x + y + 6z = 9$
 $8x + 3y + 2z = 13$
 $x + 5y + z = 7$
5. (a) Construct Newton's forward interpolation polynomial for the following data : 7

x	:	4	6	8	10
y	:	1	3	8	16
- (b) Given $u_1 = 40$, $u_3 = 45$, $u_5 = 54$, find u_2 and u_4 . 7
6. (a) Derive Lagrange's interpolation formula. 7
(b) Given the values 7

x	:	5	7	11	13	17
$f(x)$:	150	392	1452	2366	5202

Evaluate $f(a)$ using Lagrange's formula.
7. (a) Evaluate $\int_0^5 \frac{dx}{4x + 5}$ using Simpson's 7
 $\frac{1}{3}^{\text{rd}}$ rule by dividing the range into 10 equal parts. Deduce the value of \log_e^5 .

(b) Using Runge-Kutta method, solve 7

$$\frac{dy}{dx} = x^2 + y^2, \quad y(0) = 1, \quad \text{compute } y(0.2)$$

taking $h = 0.1$.

8. Explain **any four** of the following : **3.5x4=14**

- (a) Secant method
 - (b) Cramers rule
 - (c) Finite difference operators
 - (d) Types of Error
 - (e) Brents method
 - (f) Linear programming
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