B.Tech. COMPUTER SCIENCE AND ENGINEERING (BTCSVI)

Term-End Examination

June, 2013

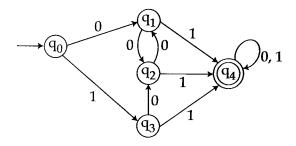
BICS-010 : FORMAL LANGUAGES AND AUTOMATA

Time: 3 hours

Maximum Marks: 70

Note: Attempt any seven questions.

- 1. (a) Design a finite automata (FA) to accept the Language L over $\{a, b\}$ such that $L = \{a^n b^n \mid n,m \ge 0 \text{ and } n+m \text{ is even}\}$
 - (b) Construct a minimum state automaton 5 equivalence to the following diagram:



2. (a) Using pumping Lemma prove that the language $L = \{o^s | s \text{ is a perfect square}\}$ is not regular.

- (b) Design a CFG for the language L over {0,1} 5to generate all possible strings of even length.
- 3 (a) Prove that the language $L = \{0^n \ 1^n \ 2^n | n \ge 1\}$ is not a Context free Language (CFL).
 - (b) Convert the CFG $G = (\{S,A,B\}, \{a, b\}, P, S)$ 5 with its production set P as $S \rightarrow aA|bB$ $A \rightarrow bAA|a, B \rightarrow BBa|b$ to Chomsky Normal form (CNF).
- **4.** What is Push down automata (PDA)? Design a PDA M to accept the Language $L = \{a^nb^{2n}|n \ge 1\}$. **4+6**
- 5. For the following PDA M, design the 10 corresponding CFG -

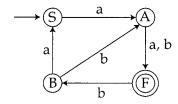
The transition functions for the PDA is as follows -

$$\delta$$
 $(q_0, a, z_0) \vdash (q_0, az_0), \delta$ $(q_1, a, a) \vdash (q_2, \epsilon)$

$$\delta$$
 $(q_0, a, a) \vdash (q_0, aa), \delta$ $(q_2, a,a) \vdash (q_2, \epsilon)$

$$\delta$$
 (q_o, c, a) \vdash (q₁, a,) δ (q₂, ϵ , z_o) \vdash (q₂, ϵ)

- 6. (a) Differentiate between a recursive and recursively enumerable language and also give the example of a language that is neither recursive nor recursively enumerable.
 - (b) What is CYK algorithm? Explain it with 5 suitable application.
- 7. (a) Prove that the language $L = \{0^n, 1^n 2^n | n \ge 1\}$ is not a CFL and also explain Pumping Lemma for context free grammars.
 - (b) Design a DFA for the Regular expression $(0+1)(01)^*(011)^*$.
- What is Turing machine? Design a Turing machine (TM) which will compute 2's complement of a binary number.
- 9. (a) Find the regular expression (RE) 5 corresponding to the following finite automata -



(b) Differentiate between Moore and Mealy machine, with the help of suitable example.

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10. Write short notes on any two:

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- (a) Church Turing thesis
- (b) Universal Turing machine
- (c) Undecidability and Reducibility

BICS-010