B.Tech. Civil (Construction Management) / B.Tech. Civil (Water Resources Engineering)

Term-End Examination June, 2012

ET-302(A): COMPUTER PROGRAMMING AND NUMERICAL ANALYSIS

Time: 3 hours Maximum Marks: 70

Note: Attempt any five questions. All questions carry equal marks. Use of calculator is permitted.

- 1. (a) If $A = \begin{bmatrix} 1 & 2 \\ 2 & 3 \\ 4 & 5 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \end{bmatrix}$ write 7+7 a program to find product of A and B.
 - (b) Given an array of numbers draw a flow chart and a program to locate the position of the largest number. Print its value and the corresponding rank position.
- 2. (a) Explain different types of file structures. 7+7 How these files are created and used?

(b) Suppose you are given three sides of a triangle A, B, C. The area of the triangle is given by

Area =
$$\sqrt{S(S-A)(S-B)(S-C)}$$

Where
$$S = (A + B + C)/2$$

However when all the sides are equal, that is triangle is equilateral, its area can be computed as $\sqrt{3(A^2)/4}$ where A is a side.

Write a program which tests whether triangle is equilateral and then compute the area accordinaly.

3. (a) Write the Syntax of :

7+7

- (i) 'Do' statement
- (ii) 'If then else' statement
- (iii) Open file and close file
- (iv) 'Continue' statement
- (b) Explain with examples the difference between:
 - (i) Function and subroutine
 - (ii) STOP and END statements
 - (iii) real variable and integer variable
 - (iv) Constant and variable

- 4. (a) Find the real root of the equation 7+7 $x \log_{10} x = 1.2$ by Bisection method correct to four decimal places.
 - (b) Evaluate $\sqrt{12}$ to four decimal places by Newton Raphson method.
- 5. (a) Use Lagrange's interpolation formula to fit 7+7 a polynomial to the data:

$$x: -1 \ 0 \ 2 \ 3$$

$$f(x): -8 \quad 3 \quad 1 \quad 12$$

Hence or otherwise find the value of f (1)

(b) Solve the following system by the LU factorization method:

$$2x + 3y + z = 9$$

$$x + 2y + 3z = 6$$

$$3x + y + 2z = 8$$

6. (a) Use Gauss-Seidel iterative method to solve 7+7 the following system of simultaneous equations

$$9x + 4y + z = -17$$

$$x - 2y - 6z = 14$$

$$x + 6y = 4$$

perform four iterations

(b) Evaluate
$$\int_0^1 \frac{dx}{1+x^2}$$
, using:

- (i) Simpson's $\frac{1}{3}$ rule taking $h = \frac{1}{4}$
- (ii) Simpson's $\frac{3}{8}$ rule taking $h = \frac{1}{6}$

Hence compute and approximate value of π in each case.

7. (a) Given
$$\frac{dy}{dx} = y - x$$
, $y(0) = 2$ 7+7

Find y(0.1) and y(0.2) correct to four decimal places.

- (b) Define operators Δ , E and ∇ . Prove the relations :
 - (i) $\nabla = 1 E^{-1}$
 - (ii) $E = e^{hD}$
 - (iii) $\Delta = E \nabla$

8. (a) Using Taylor's expansion for sin
$$x$$
 about 7+7 $x = 0$, find the approximate value of $Sin 10^{\circ}$ with errors less than 10^{-7} .

(b) Find the smallest eigen value in magnitude and the corresponding eigen vector of the matrix

$$\mathbf{A} = \begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix}$$