B.Tech. IN COMPUTER SCIENCE AND

Term-End Examination
June, 2012

## BICS-010 : FORMAL LANGUAGES AND AUTOMATA

Time : $\mathbf{3}$ hours
Maximum Marks : 70
Note : Attempt any seven questions.

1. (a) Is the language $\left\{a^{n} b a^{m} b a^{n+m} \mid n, m \geqslant 1\right\} \quad 6$ regular? Prove your claim.
(b) Show that if L is regular language, then the 4 language $\mathrm{L}^{n}$ is regular for all $n \geqslant 0$.
2. Write a grammar for the language :
$\left\{a^{n} b^{n} c^{n}: n \geqslant 0\right\}$.
3. (a) Prove or disprove the following statements

5 about regular expressions :
(i) $(R+S)^{*}=R^{*}+S^{*}$
(ii) $\quad(\mathrm{RS}+\mathrm{R})^{*} \mathrm{RS}=\left(\mathrm{RR} \mathrm{R}^{*}\right)^{*}$
(b) Explain with example the algebraic laws for 5
regular expressions.
4. Explain the difference between deterministic and $\mathbf{1 0}$ non - deterministic Push Down Automata giving their definition. Illustrate with an example of each.
5. Construct PDA for the following
$\mathrm{L}=\left\{a^{n} c b^{n} \mid n \geqslant 1\right\}$ over the alphabet $\mathrm{S}=\{a, b, c\}$
6. (a) Construct a DFA from the given NFA with

5 $S$ moves:

(b) Draw a moore or mealy machine that generates out put 'yes' when accepts a set of string from $(0+1)^{*}$ terminating in last two same symbols.
7. Let $\mathrm{F}_{1}$ and $\mathrm{F}_{2}$ are two natural function which are computed by TMS $\mathrm{M}_{1}$ and $\mathrm{M}_{2}$ respectively. Construct a TM that computes $\max \left(\mathrm{F}_{1}, \mathrm{~F}_{2}\right)$.
8. (a) State Myhill-Nerode theorem. 5
(b) Convert the given grammar in Chomsky Normal Form (CNF)

$$
\begin{aligned}
& \mathrm{S} \rightarrow \mathrm{ABa} \\
& \mathrm{~A} \rightarrow \mathrm{aab} \\
& \mathrm{~B} \rightarrow \mathrm{Ac}
\end{aligned}
$$

9. Find the regular expression corresponding to 10 given digraph.

10. Write short notes on any two :
(a) Pumping Lemmas
(b) Turning Machine Halting problem
(c) Undecidability.
