## B.Sc. (NAUTICAL SCIENCE)

Term-End Examination
June, 2012

## BNA-011 : APPLIED MATHEMATICS

Time : $\mathbf{2}$ hours
Maximum Marks : 70
Note: (i) Attempt any five question.
(ii) Use of calculator is permitted.

1. (a) Find a vector of magnitude 19 and which is perpendicular to both the vector

$$
4 \hat{i}-\hat{j}+8 \hat{k} \text { and }-\hat{j}+\hat{k}
$$

(b) Find $\int_{1}^{11} f(x) \mathrm{d} x$, where $f(x)$ is given by 7 the following table, using Simpson's one-third rule.

| $x:$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x): 543$ | 512 | 501 | 489 | 453 | 400 | 352 | 310 | 250 | 172 | 95 |  |

2. (a) An insurance company insured 2000 scooter drivers, 4000 car drivers and 6000 truck drivers. The probability of an accident involving a scooter driver, car driver and a truck is $0.01,0.03$ and 0.15 respectively, one of the insured person meets with an accident. What is the probability that he is a scooter driver ?
(b) For 10 observations on price ( $x$ ) and supply
(y), the following data were obtained (in appropriate units) :
$\Sigma x=130, \Sigma y=220, \Sigma x^{2}=2288$,
$\Sigma y^{2}=5506$ and $\Sigma x y=3467$ obtain the $y$ on $x$ line of regression.
3. (a) If $x \sqrt{1+y}+y \sqrt{1+x}=0$ for $-1<x<1 \quad 7$
prove that $\frac{\mathrm{d} y}{\mathrm{~d} x}=\frac{-1}{(1+x)^{2}}$
(b) If $x=\mathrm{a}(\cos \mathrm{t}+\mathrm{t} \sin \mathrm{t})$ and $y=(\sin \mathrm{t}-\mathrm{t} \cos \mathrm{t})$,
find $\frac{\mathrm{d}^{2} y}{\mathrm{~d} x^{2}}$
4. (a) Evaluate $\int \frac{1-\tan x}{1+\tan x} \mathrm{~d} x$
(b) Using integration, find the area of the region 7 bounded between the line $x=4$ and the parabola $y^{2}=16 x$.
5. (a) In a spherical triangle PQR angles $\mathrm{P}, \mathrm{Q}$ and 7 R are $58^{\circ} 30^{\prime}, 100^{\circ} 24^{\prime}$ and $74^{\circ} 00^{\prime}$ respectively. Calculate side $p$.
(b) In a quadrantal spherical triangle ABL , side 7 $\mathrm{b}=90^{\circ}$ angles $A$ and $B$ are $65^{\circ} 30^{\prime}$ and $75^{\circ} 15^{\prime}$ respectively. Calculate side c and angle C .
6. (a) Find the equation of the ellipse given foci 7 $( \pm 3,0)$ and passing through $(4,1)$.
(b) Find the equation of the circle of radius 7 5 whose centre lies on $x$-axis and passes through the point $(2,3)$.
