

BACHELOR IN COMPUTER APPLICATIONS

Term-End Examination

June, 2012

CS-60 : FOUNDATION COURSE IN
MATHEMATICS IN COMPUTING

Time : 3 hours

Maximum Marks : 75

Note : Question No. 1 is compulsory. Attempt any three questions from question No. 2 to 6. Use of calculator is permitted.

1. (a) If f is a real function defined by $f(x) = \frac{x-1}{x+1}$

then prove that $f(2x) = \frac{3f(x)+1}{f(x)+3}$. 15x3=45

(b) Find the inverse relation R^{-1} in each of the following cases :

(i) $R = \{ (1, 2), (1, 3), (2, 3), (3, 2), (5, 6) \}$

(ii) $R = \{ x, y \} : x, y \in \mathbb{N}, x+2y=8 \}$

(iii) R is a relation from $\{11, 12, 13\}$ to $\{8, 10, 12\}$ defined by $y=x-3$.

(c) Show that the function $f : \mathbb{R} \rightarrow \mathbb{R}$ defined as $f(x) = 5x + 4 \forall x \in \mathbb{R}$ is one - one and onto.

- (d) Find $\frac{dy}{dx}$ if $xy + y^2 + 3x^2y^3 + 4x^3 + 5 = 0$
- (e) Evaluate $\int_3^5 (9x^2 + 4x + 5) dx$.
- (f) Show that the four points $(0, -1)$, $(6, 7)$, $(-2, 3)$ and $(8, 3)$ are the vertices of a rectangle.
- (g) Find the slope of a line which passes through the points $(3, 2)$ and $(-1, 5)$.
- (h) Find the centre and radius of the given circle $x^2 + y^2 - 4x + 6y = 12$.
- (i) Find the equation of the parabola whose focus is $(-3, 2)$ and the directrix is $x + y = 4$.
- (j) Find the equation of the ellipse whose eccentricity is $\frac{1}{2}$, the focus is $(-1, 1)$ and the directrix is $x - y + 3 = 0$.
- (k) Find the equation of the hyperbola whose directrix is $2x + y = 1$, focus is $(1, 2)$ and eccentricity is $\sqrt{3}$.
- (l) Let $V = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$, $A = \{1, 2, 3, 4\}$, $B = \{2, 4, 6, 8\}$, $C = \{3, 4, 5, 6\}$ find (i) $(A \cap C)'$ (ii) $(A \cup B)'$ (iii) $(B - C)'$
- (m) Solve the simultaneous equations $x - y = 5$; $3x + 7y = 5$.
- (n) Find the real numbers x and y if $(x - iy)$ $(3 + 5i)$ is the conjugate of $-6 - 24i$.
- (o) Evaluate $\int x^3 \sin(x^4 + 1) dx$

2. (a) Find the equation of the plane through the points $(2, 1, -1)$ and $(-1, 3, 4)$ and perpendicular to the plane $x - 2y + 4z = 10$.
- (b) Find the path traced by the centre of a sphere which touches the lines $y = x, z = 1$ and $y = -x, z = -1$.
- (c) Find the equation of the cylinder having for its base the circle $x^2 + y^2 + z^2 = 9$; $x - y + z = 3$. 3+4+3

3. (a) If α and β are the roots of the equation $2x^2 - 6x + 2 = 0$. Form the equation whose roots are $\frac{1 - \alpha}{1 + \alpha}$ and $\frac{1 - \beta}{1 + \beta}$. 3+3+4

(b) Prove that $(A - B) \cup B = A \cup B$.

- (c) Express the given complex number in the polar form $\frac{2 + 6\sqrt{3}i}{5 + \sqrt{3}i}$.

4. (a) Evaluate : $\int (4x + 5)^6 dx$. 3+3+4

(b) Evaluate : $\int (\log x)^2 dx$.

- (c) If $y = \left[x + \sqrt{x^2 + a^2} \right]^n$. Prove that

$$\frac{dy}{dx} = \frac{ny}{\sqrt{x^2 + a^2}}$$

5. (a) Find the equation of the circle through the points of intersection of the circles $x^2 + y^2 + 2x + 3y - 7 = 0$ and $x^2 + y^2 + 3x - 2y - 1 = 0$ and passes through the point $(1, 2)$. 4+3+3
- (b) Obtain the equation of the parabola whose vertex is at $(a, 0)$ and focus is at $(b, 0)$ ($b \neq 0$).
- (c) Find the co - ordinates of the centre, foci and length of the latus rectum and equations of the directrices of the ellipse $\frac{(x - 2)^2}{25} + \frac{(y + 3)^2}{16} = 1$.
6. (a) Determine the local maximum and local minimum of the function $x^3 - 7x^2 + 8x + 32$.
- (b) Find the point on the curve $y = 2x^2 - 6x - 4$ at which the tangent is parallel to the x - axis. 3+4+3
- (c) Find the equation of the normal to the curve $y = 2x^2 + 3 \sin x$ at $x = 0$.
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