# M. Sc. (MATHEMATICS WITH APPLICATIONS IN COMPUTER SCIENCE) M. Sc. (MACS) <br> Term-End Examination <br> December, 2022 <br> MMTE-003 : PATTERN RECOGNITION AND IMAGE PROCESSING 

Time : 2 Hours<br>Maximum Marks : 50

Note : Attempt any five questions. All questions carry equal marks. Use of calculator is not allowed. Symbols used have their usual meaning.

1. (a) What is histogram equalization ? Does discrete histogram equalization, yield a uniform histogram ? Justify your answer. 4
(b) Briefly discuss Discrete Fourier Transform (DFT). Apply DFT to the following sequence ' $x$ ' and verify whether it works : 6

$$
x=\{1,2,8,9\}
$$

2. (a) How Bayesian classifier performs classification ? Discuss. Apply the Bayesian classifier on the following dataset, and predict the class of $(2,2): \quad 6$

| $a_{1}$ | $a_{2}$ | Class (i) |
| :---: | :---: | :---: |
| 2 | 0 | $\mathrm{C}_{1}$ |
| 0 | 2 | $\mathrm{C}_{1}$ |
| 2 | 4 | $\mathrm{C}_{2}$ |
| 0 | 2 | $\mathrm{C}_{2}$ |
| 3 | 2 | $\mathrm{C}_{2}$ |

(b) What are Median filters ? Compute the median value of the pixel circled below, using the $3 \times 3$ mask $\left[\begin{array}{ccc}1 & 5 & 7 \\ 2 & 4 & 6 \\ 3 & 2 & 1\end{array}\right]$.
3. (a) Write formula for MSE, SNR and PSNR, use them to compute MSE, SNR and PSNR for the 8 bit reference image given below : 6

$$
\begin{aligned}
f(x, y) & =\left[\begin{array}{lll}
3 & 2 & 1 \\
1 & 2 & 1 \\
3 & 2 & 2
\end{array}\right] \\
\text { and } \quad \hat{f}(x, y) & =\left[\begin{array}{lll}
3 & 1 & 1 \\
1 & 1 & 2 \\
1 & 1 & 1
\end{array}\right]
\end{aligned}
$$

(b) Give two similarities and two differences between spatial convolution and spatial correlation. 4
4. (a) Compare Weiner filtering with inverse filtering. Give limitations of Inverse filtering and describe how Weiner filter overcome the identified limitations of inverse filtering. 4
(b) What is 'Huffman Coding' ? Calculate the number of bits required to code the data given below, by using Huffman coding : 6

| Symbol | Frequency |
| :---: | :---: |
| $a$ | 21 |
| $b$ | 16 |
| $c$ | 15 |
| $d$ | 18 |
| $e$ | 32 |
| $f$ | 8 |

P.T. O.
5. (a) State whether the following statements are true or false. Give reason for your answer :

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(i) 2-D Gaussian operator is separable
(ii) Laplacian of a Gaussian operator is non-separable
(b) What is Radon transformation ? Show that the Radon transform of Gaussian shape $f(x, y)=\mathrm{A} e^{-\left(x^{2}+y^{2}\right)}$ is $g(\rho, \theta)=\mathrm{A} \sqrt{\pi} e^{-\rho^{2}}$. 6
6. (a) Distinguish between the decision-theoretic approach and the structural approach of Pattern recognition. Give suitable example for each.
(b) What is KL transform ? Compute the KL transform for the input data:

$$
\begin{aligned}
& \mathrm{X}_{1}=(4,4,5)^{\mathrm{T}} \\
\mathrm{X}_{2} & =(3,2,5)^{\mathrm{T}} \\
\mathrm{X}_{3} & =(5,7,6)^{\mathrm{T}} \\
\text { and } \quad & \mathrm{X}_{4}
\end{aligned}=(6,7,7)^{\mathrm{T}} .
$$

7. (a) What is digital image watermarking ? Draw and discuss block diagram for embedding and extraction of a digital image watermark.
(b) Consider the following five training sets as shown below :

4

| S. No. | Inputs |  | Output |
| :---: | :---: | :---: | :---: |
|  | $\mathrm{I}_{1}$ | $\mathrm{I}_{2}$ | 0 |
| 1 | 0.4 | -0.7 | 0.1 |
| 2 | 0.3 | -0.5 | 0.05 |
| 3 | 0.6 | 0.1 | 0.3 |
| 4 | 0.2 | 0.4 | 0.25 |
| 5 | 0.1 | -0.2 | 0.12 |

(i) Draw the neural network architecture.
(ii) Obtain the updated weights, error and training set for second iteration.

