No. of Printed Pages : 5 MMTE-003

M. Sc. (MATHEMATICS WITH APPLICATIONS IN COMPUTER SCIENCE) M. Sc. (MACS) Term-End Examination December, 2022 MMTE-003 : PATTERN RECOGNITION AND IMAGE PROCESSING

Time : 2 Hours

Maximum Marks : 50

Note: Attempt any five questions. All questions carry equal marks. Use of calculator is not allowed. Symbols used have their usual meaning.

- (a) What is histogram equalization ? Does discrete histogram equalization, yield a uniform histogram ? Justify your answer. 4
 - (b) Briefly discuss Discrete Fourier Transform (DFT). Apply DFT to the following sequence 'x' and verify whether it works : 6

 $x = \{1, 2, 8, 9\}$

2. (a) How Bayesian classifier performs classification ? Discuss. Apply the Bayesian classifier on the following dataset, and predict the class of (2, 2) : 6

<i>a</i> ₁	a_2	Class (i)
2	0	C_1
0	2	C_1
2	4	C_2
0	2	C_2
3	2	C_2

(b) What are Median filters ? Compute the median value of the pixel circled below,

using the
$$3 \times 3$$
 mask $\begin{bmatrix} 1 & 5 & 7 \\ 2 & 4 & 6 \\ 3 & 2 & 1 \end{bmatrix}$. 4

 (a) Write formula for MSE, SNR and PSNR, use them to compute MSE, SNR and PSNR for the 8 bit reference image given below :6

$$f(x, y) = \begin{bmatrix} 3 & 2 & 1 \\ 1 & 2 & 1 \\ 3 & 2 & 2 \end{bmatrix}$$

and $\hat{f}(x, y) = \begin{bmatrix} 3 & 1 & 1 \\ 1 & 1 & 2 \\ 1 & 1 & 1 \end{bmatrix}$

- (b) Give two similarities and two differences between spatial convolution and spatial correlation.
- 4. (a) Compare Weiner filtering with inverse filtering. Give limitations of Inverse filtering and describe how Weiner filter overcome the identified limitations of inverse filtering.
 - (b) What is 'Huffman Coding' ? Calculate the number of bits required to code the data given below, by using Huffman coding : 6

Symbol	Frequency	
a	21	
b	16	
с	15	
d	18	
e	32	
f	8	

5. (a) State whether the following statements are true *or* false. Give reason for your answer :

4

- (i) 2-D Gaussian operator is separable
- (ii) Laplacian of a Gaussian operator is non-separable
- (b) What is Radon transformation ? Show that the Radon transform of Gaussian shape $f(x, y) = Ae^{-(x^2 + y^2)}$ is $g(\rho, \theta) = A\sqrt{\pi} e^{-\rho^2}$. 6
- 6. (a) Distinguish between the decision-theoretic approach and the structural approach of Pattern recognition. Give suitable example for each.
 - (b) What is KL transform ? Compute the KL transform for the input data : 6

$$\begin{split} X_1 &= (4,4,5)^T \\ X_2 &= \left(3,2,5\right)^T \\ X_3 &= \left(5,7,6\right)^T \\ \text{and} & X_4 &= \left(6,7,7\right)^T. \end{split}$$

- 7. (a) What is digital image watermarking ?
 Draw and discuss block diagram for embedding and extraction of a digital image watermark.
 - (b) Consider the following five training sets as shown below :

S. No.	Inputs		Output
	I_1	I_2	0
1	0.4	-0.7	0.1
2	0.3	-0.5	0.05
3	0.6	0.1	0.3
4	0.2	0.4	0.25
5	0.1	-0.2	0.12

- (i) Draw the neural network architecture.
- (ii) Obtain the updated weights, error and training set for second iteration.

MMTE-003