MSTL-002/S1

## POST GRADUATE DIPLOMA IN APPLIED STATISTICS (PGDAST)

## Term-End Examination



December, 2017
MSTL-002/S1 : INDUSTRIAL STATISTICS LAB SET-1
Time : 3 Hours
Maximum Marks : 50
Note: (i) Attempt any two questions.
(ii) Solve the questions in Microsoft Excel.
(iii) Use of Formulae and Statistical Tables Booklet for PGDAST is allowed.
(iv) Mention necessary steps, hypotheses, interpretation, etc.
(v) Symbols have their usual meanings.

1. (a) A process for manufacture of 4 -feet by 8 -feet wood grain panels has performed with an average of 2.7 imperfections per 100 panels. Construct a suitable chart to be used in the inspection of the panels and discuss whether the process is under statistical control, if 25 successive 100-panel lots contained the following number of imperfect panels per lot :
$4,1,0,3,5,3,6,4,1,4,0,1,4,2,3,8,4,2,1,3,0,2,6,1,3$ Also compute the revised central line and control limits and plot the revised control chart, if necessary.
(b) A multinational company fills mango juice into cans, advertising as containing 200 ml of the juice. The weights of the juice are taken immediately after filling in the cans and 20 samples each of 4 cans are taken by a random method at an interval of 30 minutes. The sample values are tabulated in the table given below :

| Sample No. | Weight of each can (in ml) |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 215 | 212 | 213 | 220 |
| 2 | 210 | 208 | 208 | 214 |
| 3 | 208 | 215 | 217 | 210 |
| 4 | 212 | 217 | 211 | 212 |
| 5 | 218 | 215 | 213 | 204 |
| 6 | 220 | 216 | 214 | 220 |
| 7 | 225 | 219 | 223 | 220 |
| 8 | 213 | 223 | 214 | 216 |


| Sample No. | Weight of each can (in ml) |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 9 | 209 | 208 | 218 | 205 |
| 10 | 206 | 208 | 224 | 222 |
| 11 | 205 | 212 | 220 | 215 |
| 12 | 203 | 215 | 218 | 218 |
| 13 | 206 | 218 | 212 | 210 |
| 14 | 212 | 209 | 215 | 218 |
| 15 | 215 | 215 | 206 | 216 |
| 16 | 218 | 217 | 208 | 215 |
| 17 | 213 | 216 | 205 | 204 |
| 18 | 210 | 220 | 208 | 210 |
| 19 | 205 | 215 | 210 | 212 |
| 20 | 206 | 214 | 212 | 214 |

(i) Which control charts should be used to control the process mean and range of weight of juice filled in cans?
(ii) Construct these charts and check whether the process is under statistical quality control.
(iii) Also plot the revised control charts, if necessary.
2. A company wants to test the effect of age and gender on productivity in terms of units produced by its employees per month. The HR Manager has taken a random sample of 15 employees and collected information about their age and gender as given below :

| Employee | Productivity | Age | Gender |
| :---: | :---: | :---: | :---: |
| 1 | 850 | 40 | Male |
| 2 | 760 | 34 | Female |
| 3 | 750 | 28 | Female |
| 4 | 860 | 34 | Male |
| 5 | 800 | 38 | Female |
| 6 | 710 | 26 | Male |
| 7 | 760 | 31 | Male |
| 8 | 860 | 38 | Male |
| 9 | 770 | 31 | Male |
| 10 | 800 | 30 | Male |
| 11 | 870 | 38 | Male |
| 12 | 800 | 28 | Male |
| 13 | 750 | 31 | Female |
| 14 | 840 | 37 | Male |
| 15 | 760 | 31 | Female |

For this data :
(a) Prepare a scatter plot to get an idea about the relationship among the variables.
(b) Develop a linear regression model and its related analysis at $2 \%$ level of significance.
(c) Draw both fitted regression lines on the scatter plot.
(d) Determine the productivity for the male employee of age 35 years.
3. A meteorologist has taken the data of annual rainfall (in cm ) in the region of a particular State from 1970 to 2010. The data is given in the following table :

| Year | Rainfall | Year | Rainfall | Year | Rainfall | Year | Rainfall |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1970 | 664 | 1981 | 548 | 1991 | 624 | 2001 | 468 |
| 1971 | 728 | 1982 | 417 | 1992 | 473 | 2002 | 554 |
| 1972 | 447 | 1983 | 387 | 1993 | 750 | 2003 | 744 |
| 1973 | 663 | 1984 | 590 | 1994 | 343 | 2004 | 943 |
| 1974 | 630 | 1985 | 556 | 1995 | 484 | 2005 | 582 |
| 1975 | 451 | 1986 | 292 | 1996 | 545 | 2006 | 581 |
| 1976 | 617 | 1987 | 327 | 1997 | 419 | 2007 | 437 |
| 1977 | 734 | 1988 | 494 | 1998 | 798 | 2008 | 417 |
| 1978 | 491 | 1989 | 448 | 1999 | 334 | 2009 | 617 |
| 1979 | 520 | 1990 | 704 | 2000 | 465 | 2010 | 571 |
| 1980 | 280 |  |  |  |  |  |  |

(a) Use the exponential smoothing method with $\alpha=0.5$ and obtain the smoothed series of observations.
(b) Plot the original and smoothed values in the chart.
(c) Compute the seasonal indices using 4-yearly ratio to moving average method.

