# B.Tech. - VIEP - COMPUTER SCIENCE AND ENGINEERING (BTCSVI) 

## ロロ347 <br> Term-End Examination

December, 2017

## BICS-010 : FORMAL LANGUAGES AND AUTOMATA

Time : 3 hours
Maximum Marks : 70

Note: Attempt any seven questions. All questions carry equal marks.

1. (a) Design a DFA to accept the language $L=\{\mathbf{w} \mid w$ has $3 k+1$ b's for some $k \in N\}$ over alphabets $\Sigma=\{a, b\}$ (where $N$ is a natural number). 5
(b) Prove $L=\left\{w \in(0,1)^{*} \mid w\right.$ contains the same number of 0 's and 1 's) is non-regular using pumping lemma. 5
2. Construct a minimum state automaton equivalent to the following diagram :

3. Prove that the following language is not a CFL by pumping lemma :

$$
\mathrm{L}=\left\{\mathrm{a}^{\mathrm{n}} \mathrm{a}^{\mathrm{n}+1} \mathrm{c}^{\mathrm{n}+2} \mid \mathrm{n} \geq 0\right\}
$$

4. Write the definition of Moore Machine and convert the following Mealy Machine into equivalent Moore Machine :

| Present <br> State | Next State |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{a}=0$ |  | $\mathrm{a}=1$ |  |
|  | Next <br> state | Output | Next <br> state | Output |
| $\rightarrow \mathrm{a}$ | d | 0 | b | 1 |
| b | a | 1 | d | 0 |
| c | c | 1 | c | 0 |
| d | b | 0 | a | 1 |

5. Define Turing Machine. Design a Turing Machine that accepts the following language :

$$
L=\left\{a^{n+1} b^{n} \mid n>0\right\}
$$

6. (a) For the given state diagram of a NFA, find the equivalent DFA.

$$
5
$$


(b) Construct a DFA from the given NFA with $\varepsilon$ moves.

7. Convert the following context-free grammar to Greibach Normal Form (GNF) :

$$
\begin{aligned}
& \mathrm{S} \rightarrow \mathrm{AB} \mid \mathrm{BC} \\
& \mathrm{~A} \rightarrow \mathrm{AB} \mid \mathrm{a} \\
& \mathrm{~B} \rightarrow \mathrm{AA}|\mathrm{CB}| \mathrm{b} \\
& \mathrm{C} \rightarrow \mathrm{a} \mid \mathrm{b}
\end{aligned}
$$

8. Let $f_{1}$ and $f_{2}$ be two natural functions which are computed by TM $\mathrm{M}_{1}$ and $\mathrm{M}_{2}$ respectively. Construct a TM that computes $\max \left(\mathrm{f}_{1}, \mathrm{f}_{2}\right)$. 10
9. Define DPDA. Design a PDA for recognizing

$$
\begin{aligned}
& \mathrm{L}=\left\{\mathrm{a}^{\mathrm{m}} \mathrm{~b}^{\mathrm{n}} \mathrm{c}^{0} \mathrm{~d}^{\mathrm{p}} \mid \mathrm{m}, \mathrm{n}, \mathrm{o}, \mathrm{p} \geq 1\right. \text { and } \\
& \mathrm{m}+\mathrm{n}=\mathrm{o}+\mathrm{p}\} .
\end{aligned}
$$

10. Write short notes on any two of the following : $2 \times 5=10$
(a) Variants of Turing Machine
(b) Post Correspondence Problem
(c) Chomsky Hierarchy
(d) Recursive and Recursively Enumerable Languages
