# POST GRADUATE DIPLOMA IN APPLIED STATISTICS (PGDAST) 

Term-End Examination 00947

## December, 2015

## MSTL-002 : INDUSTRIAL STATISTICS LAB

Note : (i) Attempt any two questions.
(ii) Solve the questions in Microsoft Excel.
(iii) Use of Formulae and Statistical Tables Booklet for PGDAST is allowed.
(iv) Mention necessary steps, hypotheses, interpretation, etc.

1. (a) Suppose a dairy product manufacturing $\mathbf{1 5}$ company uses automatic machines to fill 500 mL flavoured milk bottles. A quality control inspector at the company collects 20 samples each of four observations at different times and measures the volume of each filled bottle. The data are given in the following table :

Table : Volume of Flavoured Milk

| Sample <br> Number | Volume of flavoured milk per bottle (in mL) |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Obs. 1 | Obs. 2 | Obs. 3 | Obs. 4 |
| 1 | 497 | 500 | 498 | 497 |
| 2 | 505 | 500 | 498 | 500 |
| 3 | 499 | 497 | 498 | 498 |
| 4 | 499 | 496 | 498 | 497 |
| 5 | 498 | 500 | 499 | 500 |
| 6 | 499 | 500 | 499 | 500 |
| 7 | 499 | 498 | 497 | 496 |
| 8 | 499 | 498 | 500 | 498 |
| 9 | 499 | 498 | 500 | 502 |
| 10 | 498 | 497 | 499 | 498 |
| 11 | 498 | 500 | 501 | 499 |
| 12 | 498 | 501 | 500 | 499 |
| 13 | 497 | 498 | 497 | 499 |
| 14 | 499 | 498 | 498 | 501 |
| 15 | 500 | 500 | 499 | 499 |
| 16 | 500 | 500 | 499 | 498 |
| 17 | 501 | 497 | 494 | 496 |
| 18 | 499 | 500 | 501 | 498 |
| 19 | 499 | 500 | 499 | 500 |
| 20 | 497 | 498 | 499 | 497 |

Develop the $\bar{X}$ and R-charts to check whether the process of bottling is under statistical control or out-of-control. Also, plot the revised control limits, if necessary.
(b) To monitor the manufacturing of smart phones, a quality controller randomly selects number of smart phones from the production line, each day over a period of 25 days. The smart phones were inspected for defectives and the number of defective smart phones found each day are recorded in the following table:

| Day | Number of Smart Phones Inspected | Number of Defective Smart Phones |
| :---: | :---: | :---: |
| 1 | 50 | 2 |
| 2 | 52 | 4 |
| 3 | 57 | 4 |
| 4 | 50 | 11 |
| 5 | 50 | 4 |
| 6 | 48 | 2 |
| 7 | 51 | 4 |
| 8 | 54 | 6 |
| 9 | 52 | 5 |
| 10 | 50 | 1 |
| 11 | 55 | 6 |
| 12 | 60 | 3 |
| 13 | 55 | 6 |
| 14 | 55 | 5 |
| 15 | 52 | 1 |
| 16 | 48 | 4 |
| 17 | 50 | 3 |
| 18 | 56 | 6 |
| 19 | 52 | 2 |
| 20 | 53 | 4 |
| 21 | 50 | 3 |
| 22 | 55 | 1 |
| 23 | 50 | 5 |
| 24 | 50 | 3 |
| 25 | 47 | 4 |

Construct the suitable control chart and comment whether the process is under statistical control or not. Also compute the revised control limits, if necessary.
2. A sample of 20 houses was selected to develop a linear model for the electricity consumption of a household and to predict the electricity consumption during summers. We have recorded the electricity consumption (in kWh ), size of house (in Sq.ft.), and AC ( 0 for no AC and 1 for having AC ) in the following table :

Table : Electricity Consumption Data

| S. No. | Unit <br> (in kWh) | Area <br> (in Sq. ft.) | AC | S. No. | Unit <br> (in kWh) | Area <br> (in Sq. ft.) | AC |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | 513 | 725 | 1 | 11 | 736 | 825 | 1 |
| 2 | 926 | 1000 | 1 | 12 | 593 | 850 | 0 |
| 3 | 706 | 925 | 1 | 13 | 866 | 1000 | 1 |
| 4 | 1046 | 1300 | 0 | 14 | 780 | 950 | 1 |
| 5 | 1196 | 1400 | 1 | 15 | 920 | 1100 | 0 |
| 6 | 1060 | 1200 | 1 | 16 | 870 | 1100 | 0 |
| 7 | 713 | 825 | 0 | 17 | 806 | 1075 | 0 |
| 8 | 516 | 775 | 1 | 18 | 880 | 1000 | 1 |
| 9 | 373 | 675 | 0 | 19 | 666 | 875 | 1 |
| 10 | 1070 | 1350 | 0 | 20 | 820 | 1025 | 0 |

(a) Prepare a scatter plot to get an idea about the relationship among the variables.
(b) Develop a linear regression model and perform related analysis at $5 \%$ level of significance.
(c) Check the linearity and normality assumptions for the regression analysis.
(d) Draw both fitted regression lines on the scatter plot.
3. Suppose the owner of an ice-cream parlour situated in a locality of a metro city wants to analyse its monthly sales. The data of the total quantity of ice-cream sold every month for past 4 years from 2008 to 2011 are recorded in the following table :

Table : Monthly Sales of Ice-cream

| Month | Quantity <br> (in litre) | Month | Quantity <br> (in litre) | Month | Quantity <br> (in litre) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 288 | 17 | 824 | 33 | 967 |
| 2 | 316 | 18 | 802 | 34 | 924 |
| 3 | 414 | 19 | 812 | 35 | 848 |
| 4 | 540 | 20 | 776 | 36 | 774 |
| 5 | 558 | 21 | 767 | 37 | 694 |
| 6 | 586 | 22 | 738 | 38 | 765 |
| 7 | 558 | 23 | 689 | 39 | 1134 |
| 8 | 548 | 24 | 596 | 40 | 1224 |
| 9 | 540 | 25 | 540 | 41 | 1210 |
| 10 | 565 | 26 | 630 | 42 | 1237 |
| 11 | 465 | 27 | 879 | 43 | 1248 |
| 12 | 396 | 28 | 990 | 44 | 1217 |
| 13 | 396 | 29 | 1032 | 45 | 1215 |
| 14 | 450 | 30 | 1020 | 46 | 1134 |
| 15 | 648 | 31 | 1005 | 47 | 1024 |
| 16 | 764 | 32 | 1017 | 48 | 898 |

(a) Compute the seasonal indices for the 12 months.
(b) Obtain the deseasonalised values.
(c) Plot the given data and the deseasonalised values.

