

**B.Tech. – VIEP – MECHANICAL ENGINEERING
(BTMEVI)**

Term-End Examination

December, 2015

00741

BIMEE-008 : MECHANICAL VIBRATION

Time : 3 hours

Maximum Marks : 70

*Note : Answer any **five** questions. All questions carry equal marks. Use of scientific calculator is permitted.*

1. Define any **four** of the following terms : $4 \times 3 \frac{1}{2} = 14$
- (a) Free vibration
 - (b) Forced vibration
 - (c) Periodic motion
 - (d) Degree of freedom
 - (e) Natural frequency

2. A machine of mass $m = 500 \text{ kg}$ is mounted on a simply supported steel beam of length $l = 2 \text{ m}$ having a rectangular cross-section (depth = 0.1 m , width = 1.2 m) and Young's modulus $E = 2.06 \times 10^{11} \text{ N/m}^2$. To reduce the vertical deflection of the beam, a spring of stiffness k is attached at the mid-span, as shown in Figure 1. Determine the value of k needed to reduce the deflection of the beam by (a) 25% of its original value, (b) 50% of its original value, and (c) 75% of its original value.

14

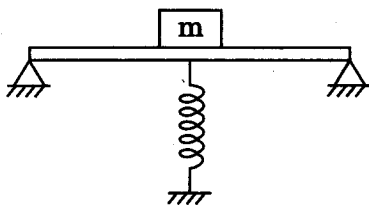


Figure 1

3. (a) Find the sum of the two harmonic motions $x_1(t) = 10 \cos(\omega t)$ and $x_2(t) = 15 \cos(\omega t + 2)$.

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- (b) A cantilever beam carries a mass M at its free end as shown in Figure 2. A mass m falls from a height h onto the mass M and adheres to it without rebounding. Determine the resulting transverse vibrations of the beam.

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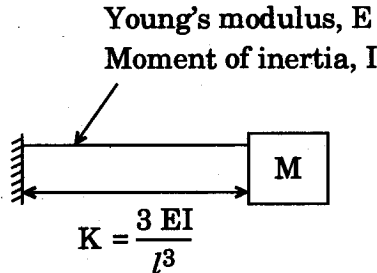


Figure 2

4. Find the equation of motion of the uniform rigid bar OA of length l and mass m shown in Figure 3. Also find its natural frequency.

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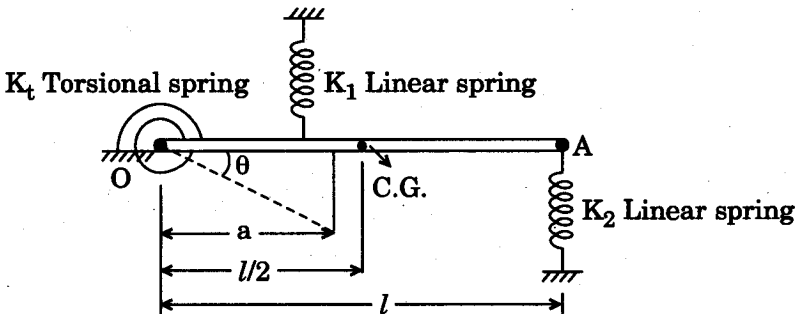


Figure 3

5. Find the total response of a single degree of freedom system with $m = 10$ kg, $C = 20$ Ns/m, $K = 4000$ N/m, $x_0 = 0.01$ m and $\dot{x}_0 = 0$ under the following conditions : 14
- (a) An external force $F(t) = F_0 \cos \omega t$ acts on the system with $F_0 = 100$ N and $\omega = 10$ rad/s.
- (b) Free vibration with $F(t) = 0$.
6. Write the equations of motion for the response of a damped system under harmonic force and derive the expression for 'Magnification factor'. Also give the main characteristics of the magnification factor. 14
7. (a) Determine the equations of motion and the natural frequencies of the system shown in Figure 4. 10

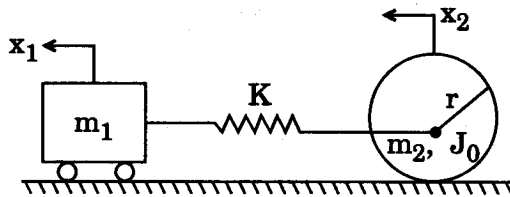


Figure 4

- (b) What is critical speed of a shaft and what is its significance ? 4

8. Find the natural frequencies of the tapered cantilever beam shown in Figure 5, using deflection shape $W(x) = \left(1 - \frac{x}{l}\right)^2$. Apply Rayleigh-Ritz method. 14

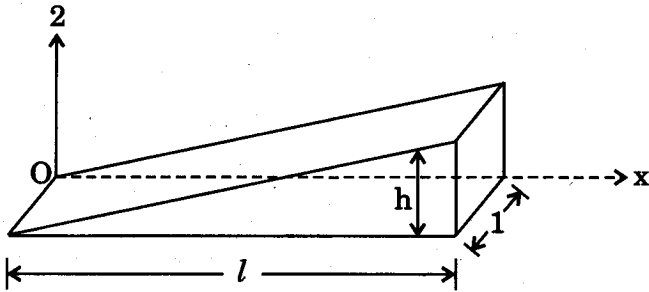


Figure 5