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ET-302(A)

B.Tech. Civil (Construction Management)/ B.Tech. Civil (Water Resources Engineering)

Term-End Examination

December, 2015

ET-302(A): COMPUTER PROGRAMMING AND NUMERICAL ANALYSIS

Time: 3 hours

Maximum Marks: 70

Note: Attempt any **five** questions. All questions carry equal marks. Use of calculator is permitted.

- 1. (a) Draw a flow chart to read 15 numbers and find out its mean and variance.
 - (b) Write a program to read two matrices A and B, both are square matrices, and check whether $A = B^{-1}$ or not.

2. (a) Write the arithmetic statement functions for the following in FORTRAN:

$$(i) \qquad \frac{x^2 - y^2}{|x - y|}$$

(ii)
$$x^2 - y^2z - zx^2 - z^2y$$

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(b) Explain the following control constructs with examples:

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- (i) IF
- (ii) DO
- (iii) CASE
- (iv) GOTO
- 3. (a) Use Lagrange's formula to compute the value of y, when x = 5, if the following values of x and y are given:

 x
 1
 2
 3
 4
 7

 y
 2
 4
 8
 16
 128

(b) Using Newton-Raphson method, find out the root of the equation correct to three decimal places

 $x \sin x + \cos x = 0$, which is near to $x = \pi$.

4. (a) Solve the following system of equations:

$$x + y + z = 1$$

$$4x + 3y - z = 6$$

$$3x + 5y + 3z = 4$$

using Gauss-Jordan method with pivoting.

(b) Calculate the value of $\int_0^{\pi} \sin x \, dx$ by Simpson's $\frac{1}{3}$ rule using 11 ordinates.

5. (a) Using Runge-Kutta method of order 4, find y(0.2) for the equation

$$\frac{dy}{dx} = \frac{y-x}{y+x}$$
; y (0) = 1.

Take h = 0.2.

(b) Find first and second derivative at 1·1 for the data

x	1.00	1.2	1.4	1.6	1.8	2.00
У	0	0.1280	0.5440	1.2960	2.432	4.00

6. (a) Determine the eigenvalues and corresponding eigenvectors for the matrix A.

$$\mathbf{A} = \begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix}.$$

(b) Find inverse of the matrix A

$$A = \begin{bmatrix} 5 & 8 & 1 \\ 0 & 2 & 1 \\ 4 & 3 & -1 \end{bmatrix}$$

and hence solve Ax = b when

$$\mathbf{b} = \begin{bmatrix} 1 \\ -2 \\ 3 \end{bmatrix}.$$

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7. (a) The following table gives the values of x and y. Use appropriate central difference formula to find the value of y when x is 38.

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x: 30 35 40 y: 15.9 14.9 14.1

 $50 \\ 12.5$

45

13.3

(b) Prove that

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- (i) $\nabla \mathbf{E} = \mathbf{E} \nabla = \Delta = \mathbf{E} \mathbf{1}$
- (ii) $e^{x} = \left(\frac{\Delta^{2}}{E}\right) e^{x} \cdot \frac{E e^{x}}{\Delta^{2} e^{x}}$, interval of differencing being unity.
- 8. Explain the following:

 $4 \times 3 \frac{1}{2} = 14$

- (a) Lagrange's Mean Value Theorem
 - (b) Round off and Truncation errors
 - (c) Numerical Integration
 - (d) Global and Local Variables