

**B.Tech. – VIEP – ELECTRONICS AND
COMMUNICATION ENGINEERING
(BTECVI)**

Term-End Examination

00788

December, 2014

BIEL-010 : DIGITAL SIGNAL PROCESSING

Time : 3 hours

Maximum Marks : 70

Note : *Attempt any seven questions. All questions carry equal marks. Use of scientific calculator is permitted. Missing data may be suitably assumed.*

1. (a) State any four important properties of DFT. 4
- (b) Plot the magnitude and phase spectrum of sampled data sequence $x(n) = \{2, 0, 0, 1\}$, which is obtained using sampling frequency of 20 kHz. Select $N = 4$. 6
2. Consider the discrete time sequence
- $x_1(n) = \{0, 1, 2, 3, 4\}$
- $x_2(n) = \{0, 1, 0, 0, 0\}$
- Compute $Y(k) = X_1(k) \cdot X_2(k)$. 10

3. Compute the FFT for the sequence $x(n) = n^2 + 1$, where $N = 8$ using DIF FFT algorithm. 10

4. Discuss the computational efficiency of radix-2 FFT algorithm. 10

5. Design a digital Butterworth filter to meet the following specifications :

$$0.8 \leq |H(e^{j\omega})| \leq 1 \quad 0 \leq \omega \leq 0.2 \pi$$

$$|H(e^{j\omega})| \leq 0.2 \quad 0.6 \pi \leq \omega \leq \pi$$

Use bilinear transformation method. 10

6. What are the different types of window functions used in the design of FIR filters ? How are they defined ? 10

7. Obtain the transformation formula for bilinear transformation to convert an analog filter into a digital filter. 10

8. A filter is to be designed with the following desired frequency response :

$$H_d(e^{j\omega}) = \begin{cases} 0 & -\frac{\pi}{4} \leq \omega \leq \frac{\pi}{4} \\ e^{-j2\omega} & \frac{\pi}{4} \leq |\omega| \leq \pi \end{cases}$$

Determine the filter coefficient $h_j(n)$ if the rectangular window function is provided. Also determine the frequency response of the designed filter. 10

9. Obtain the structure of cascade realization of the following transfer functions :

$$(i) \quad H(z) = \frac{(1 - z^{-1})^3}{\left(1 - \frac{1}{2}z^{-1}\right)\left(1 - \frac{1}{8}z^{-1}\right)} \quad 5$$

$$(ii) \quad H(z) = \frac{\left(1 + \frac{1}{4}z^{-1}\right)}{\left(1 + \frac{1}{2}z^{-1}\right)\left(1 + \frac{1}{2}z^{-1} + \frac{1}{4}z^{-2}\right)} \quad 5$$

10. Write short notes on any **two** of the following : $2 \times 5 = 10$

- (a) Goertzel Algorithm
 - (b) Comparison of Butterworth and Chebyshev filter
 - (c) IIR filters vs FIR filters
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