

**B.Tech. MECHANICAL ENGINEERING / B.Tech.
IN CIVIL ENGINEERING**

Term-End Examination

December, 2013

BICE-027 : MATHEMATICS III

Time : 3 hours

Maximum Marks : 70

Note : *Attempt any seven questions. All questions carry equal marks and are to be answered in English only.*

1. Find the Fourier series expansion of the following 10
 2π - periodic function.

$$f(x) = \begin{cases} \pi+x, & -\pi < x < 0 \\ 0, & 0 \leq x < \pi \end{cases}$$

2. Obtain the Fourier series expansion of 10
 $f(x) = 1 + x, -1 < x < 1$, and hence show that:

$$\frac{\pi}{4} = 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots$$

3. Describe Fourier transform, Fourier sine transform 10
and Forrier cosine transform with examples.

4. State convolution theorem for Fourier transform and hence evaluate the inverse Fourier transform of : 10

$$\frac{1}{12 + 7iw - w^2}$$

5. Find the complete integral of : 10

$$2xz \frac{\partial z}{\partial x} + 2yz \frac{\partial z}{\partial y} = z^2 - x^2 - y^2$$

6. Find the general solution of : 10

$$2 \frac{\partial^2 z}{\partial x^2} - \frac{\partial^2 z}{\partial x \partial y} - \frac{\partial^2 z}{\partial y^2} + \frac{\partial z}{\partial x} - \frac{\partial z}{\partial y} = e^{2x+3y}$$

7. An elastic string of length l , which is fastened at its ends $x=0$ and $x=l$, is picked up at its centre point $x = \frac{l}{2}$ to a height of $\frac{l}{2}$ and is released from the rest. Find the displacement of the string at any instant of time. 10

8. Discuss Fourier series solution of one dimensional heat equation. 10

9. Solve the Laplace equation $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$ for **10**

the temperature distribution in a rectangular plate subject to the following conditions :

$$u(0, y) = 0, u(a, y) = 0; u(x, 0) = f(x), u(x, b) = 0.$$

10. (a) Obtain a second order partial differential equation from : **10**

$$u = f(x + ct) + g(x - ct)$$

where f and g are arbitrary functions and c is a constant.

(b) Solve the partial differential equation :

$$y \frac{\partial z}{\partial x} - x \frac{\partial z}{\partial y} = 0$$
