# ASSIGNMENT BOOKLET Bachelor's Degree Programme (B.Sc.) 

MATHEMATICAL METHODS IN PHYSICS-III

Valid from January 1, 2021 to December 31, 2021

It is compulsory to submit the Assignment before filling up the Term-End Examination Form.

## Please Note

- You can take electives (56 or 64 credits) from a minimum of TWO and a maximum of FOUR science disciplines, viz. Physics, Chemistry, Life Sciences and Mathematics.
- You can opt for elective courses worth a MINIMUM OF 8 CREDITS and a MAXIMUM OF 48 CREDITS from any of these four disciplines.
- At least $25 \%$ of the total credits that you register for in the elective courses from Life Sciences, Chemistry and Physics disciplines must be from the laboratory courses. For example, if you opt for a total of 64 credits of electives in these 3 disciplines, at least 16 credits out of those $\mathbf{6 4}$ credits should be from lab courses.
- You cannot appear in the Term-End Examination of any course without registering for the course. Otherwise, your result will not be declared and the responsibility will be yours.

Dear Student,

We hope you are familiar with the system of evaluation to be followed for the Bachelor's Degree Programme. At this stage you may probably like to re-read the section on assignments in the Programme Guide for Elective Courses that the University sent you after your enrolment. A weightage of 30 per cent, as you are aware, has been earmarked for continuous evaluation which would consist of one tutor-marked assignment for this course.

## Instructions for Formatting Your Assignments

Before attempting the assignment please read the following instructions carefully.

1) On top of the first page of your TMA answer sheet, please write the details exactly in the following format:

## ENROLMENT NO.

NAME $\qquad$

ADDRESS $\qquad$

## COURSE CODE

COURSE TITLE
ASSIGNMENT NO. : $\qquad$
STUDY CENTRE : DATE :
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## PLEASE FOLLOW THE ABOVE FORMAT STRICTLY TO FACILITATE EVALUATION AND TO AVOID DELAY.

2) Use only foolscap size writing paper (but not of very thin variety) for writing your answers.
3) Leave 4 cm margin on the left, top and bottom of your answer sheet.
4) Your answers should be precise and in your own words. Do not copy answers from study material.
5) While solving problems, clearly indicate the question number along with the part being solved. Write units at each step of your calculations as done in the text because marks will be deducted for such mistakes. Take care of significant digits in your work. Recheck your work before submitting it.
6) This assignment will remain valid from January 1, 2021 to December 31, 2021. However, you are advised to submit it within 12 weeks of receiving this booklet to accomplish its purpose as a teaching-tool.

We strongly feel that you should retain a copy of your assignment response to avoid any unforeseen situation and append, if possible, a photocopy of this booklet with your response.

We wish you good luck.

# Tutor Marked Assignment <br> MATHEMATICAL METHODS IN PHYSICS-III 

Course Code: PHE-14
Assignment Code: PHE-14/TMA/2021
Max. Marks: 100
Note: Attempt all questions. Symbols have their usual meanings. The marks for each question are indicated against it.

1. a) i) Show that the matrix $B=\left(\begin{array}{rr}0 & -i \\ i & 0\end{array}\right)$ is both hermitian and unitary.
ii) Determine the eigenvalues of the matrix $A$ given below:

$$
A=\left[\begin{array}{lcc}
0 & 2 i & 3 i \\
-2 i & 0 & 6 i \\
-3 i & -6 i & 0
\end{array}\right]
$$

b) Show that the eigenvectors belonging to distinct eignenvlaues of a hermitian matrix are orthogonal to each other.
c) Verify the Caley-Hamilton theorem for the following matrix:

$$
C=\left[\begin{array}{ccc}
1 & 2 & 3 \\
2 & -1 & 4 \\
3 & 1 & 1
\end{array}\right]
$$

d) Define symmetric anti-symmetric tensors. Write down transformation law obeyed by the components of a
i) Contravarient tensor of rank 3, and
ii) Covariant tensor of rank 3 .
e) Show that set $\left\{1, w, w^{2}\right\}$ forms a cyclic group of order 3 under multiplication, where $w$ is the imaginary cube root of unity.
2. a) Obtain the analytic function whose real part is:

$$
\begin{equation*}
u(x, y)=e^{x} \cos y \tag{5}
\end{equation*}
$$

b) Evaluate the integral $\oint \frac{3 Z}{\left(Z^{2}+9\right)}$ over the circle $|Z|=4$.
c) Obtain the taylor series expansion of the function $\cos ^{2} Z$ about $Z=0$.
d) Using the method of residues, show that:

$$
\begin{equation*}
\int_{0}^{2 \pi} \frac{d \theta}{2+\cos \theta}=\frac{2 \pi}{\sqrt{3}} \tag{10}
\end{equation*}
$$

3. a) Obtain the Fourier sine and cosine transforms for the following function:

$$
f(x)=\left\{\begin{array}{cl}
1-\frac{x}{2} & 0<x<2  \tag{5+5}\\
0 & x>2
\end{array}\right.
$$

b) Determine the Laplace transform of $f(t)=\frac{1}{2 a}(\sin a t+a t \cos a t)$.
c) Solve the initial value problem

$$
\begin{equation*}
y^{\prime \prime}-2 y^{\prime}-3 y=0, \quad y(0)=1, \quad y^{\prime}(0)=7 \tag{10}
\end{equation*}
$$

4. a) Show that all the roots of $P_{n}(x)=0$ are real and lie between -1 and +1 .
b) Show that

$$
\begin{equation*}
\left(\frac{\pi x}{2}\right)^{1 / 2} J_{3 / 2}(x)=\frac{\sin x}{x}-\cos x \tag{5}
\end{equation*}
$$

c) Determine the first three coefficients in the expansion of the following function in a series of the form $\sum_{k=0}^{\infty} A_{k} P_{k}(x):$

$$
f(x)=\left\{\begin{array}{cc}
0 & -1 \leq x \leq 0  \tag{10}\\
x & 0 \leq x \leq 1
\end{array}\right.
$$

d) Obtain the first order derivative of $L_{4}(x)$ using the appropriate recurrence relations. Take $L_{0}(x)=1$ and $L_{1}(x)=1-x$.

