

**ASSIGNMENT BOOKLET
Bachelor's Degree Programme (B.Sc.)**

MATHEMATICAL METHODS IN PHYSICS-II

Valid from January 1, 2022 to December 31, 2022

**It is compulsory to submit the Assignment before filling up the
Term-End Examination Form.**

Please Note

- You can take electives (56 or 64 credits) from a minimum of TWO and a maximum of FOUR science disciplines, viz. Physics, Chemistry, Life Sciences and Mathematics.
- You can opt for elective courses worth a MINIMUM OF 8 CREDITS and a MAXIMUM OF 48 CREDITS from any of these four disciplines.
- At least 25% of the total credits that you register for in the elective courses from Life Sciences, Chemistry and Physics disciplines must be from the laboratory courses. For example, if you opt for a total of 64 credits of electives in these 3 disciplines, at least 16 credits out of those 64 credits should be from lab courses.
- You cannot appear in the Term-End Examination of any course without registering for the course. Otherwise, your result will not be declared and the responsibility will be yours.



**School of Sciences
Indira Gandhi National Open University
Maidan Garhi, New Delhi-110068**

Dear Student,

We hope you are familiar with the system of evaluation to be followed for the Bachelor's Degree Programme. At this stage you may probably like to re-read the section on assignments in the Programme Guide for Elective Courses that we sent you after your enrolment. A weightage of 30 per cent, as you are aware, has been earmarked for continuous evaluation which would consist of **one tutor-marked assignment** for this course.

Instructions for Formatting Your Assignments

Before attempting the assignment please read the following instructions carefully.

- 1) On top of the first page of your TMA answer sheet, please write the details exactly in the following format:

ENROLMENT NO. :

NAME :

ADDRESS :

.....

.....

COURSE CODE :

COURSE TITLE :

ASSIGNMENT NO. :

STUDY CENTRE : DATE :

PLEASE FOLLOW THE ABOVE FORMAT STRICTLY TO FACILITATE EVALUATION AND TO AVOID DELAY.

- 2) Use only foolscap size writing paper (but not of very thin variety) for writing your answers.
- 3) Leave 4 cm margin on the left, top and bottom of your answer sheet.
- 4) Your answers should be precise.
- 5) While solving problems, clearly indicate the question number along with the part being solved. Be precise. Write units at each step of your calculations as done in the text because marks will be deducted for such mistakes. Take care of significant digits in your work. Recheck your work before submitting it.
- 6) **This assignment will remain valid from January 1, 2022 to December 31, 2022.** However, you are advised to submit it within **12 weeks** of receiving this booklet to accomplish its purpose as a teaching-tool.

We strongly feel that you should retain a copy of your assignment response to avoid any unforeseen situation and append, if possible, a photocopy of this booklet with your response.

We wish you good luck.

Tutor Marked Assignment
MATHEMATICAL METHODS IN PHYSICS-II

Course Code: PHE-05
Assignment Code: PHE-05/TMA/2022
Max. Marks: 100

Note: Attempt all questions. Symbols have their usual meanings. The marks for each question are indicated against it.

1. Solve the following ordinary differential equations:

i) $(2y + \cos y - \cos x) dx + (2x - x \sin y) dy = 0$

ii) $\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + 5y = 0; y(0) = 1; y'(0) = -1$

iii) $\frac{d^2y}{dx^2} + 3\frac{dy}{dx} + 2y = 8 \cos 2x$ (5+10+10)

2. Newton's law of cooling states that the rate at which the temperature of the body decreases is proportional to the difference of temperature between the body and its surroundings. A cup of liquid at a temperature of 90°C is kept in a room in which the temperature is 20°C . If initially the liquid cools at the rate of 1°C per minute, calculate the time taken for the liquid to cool to a temperature of 40°C . (10)

3. A block of mass 1 kg is attached to a spring of force constant $k = 125.0 \text{ Nm}^{-1}$. The block is pulled 0.5 m from its equilibrium position and released from rest. If this spring-block apparatus is submerged in a viscous fluid medium which exerts a damping force of $30v$ (where v is the instantaneous speed of the block), determine of the position $x(t)$ of the block at time t . (10)

4. Using the power series method solve the following ODE:

$$y'' - 3xy' + y = 0 \quad (10)$$

5. Show that:

$$u = Ce^{(1-n^2\pi^2)t} \sin(n\pi x)$$

is a solution of the equation:

$$\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2} + u \quad (5)$$

6. Determine all the first and second order partial derivatives for the function:

$$f(x, y) = 3e^{xy} - \ln(xy) + x^2 \cos(4y) \quad (10)$$

7. Reduce the equation

$$\frac{\partial^2 f}{\partial t^2} = c^2 \left(\frac{\partial^2 f}{\partial r^2} + \frac{1}{r} \frac{\partial f}{\partial r} + \frac{1}{r^2} \frac{\partial^2 f}{\partial \theta^2} \right)$$

to a set of ODEs by the method of separation of variables. (10)

8. Obtain the Fourier series for the following function:

$$f(x) = \begin{cases} x + \pi & \text{for } -\pi \leq x \leq 0 \\ \pi & \text{for } 0 < x < \pi \end{cases} \quad (10)$$

9. Find the solution of the wave equation for a vibrating string of length $L = 10$ units with both its ends fixed. It is given that $c = \frac{1}{\pi}$ and

$$u(x, 0) = \sin(0.3\pi x)$$

$$\frac{\partial u}{\partial t}(x, 0) = 0 \quad (10)$$
