

## B.Sc. (NAUTICAL SCIENCE)

## Term-End Examination

December, 2012

## BNA-011 : APPLIED MATHEMATICS

Time : 2 hours

Maximum Marks : 70

*Note : (i) Attempt any five questions.**(ii) Use of calculator is permitted.*

1. (a) Find  $\lambda$  so that the two vectors  $\hat{i} + (2\lambda - 1)\hat{j} + 3\hat{k}$  and  $-3\hat{i} + 2\hat{j} - \lambda\hat{k}$  are perpendicular. 7

- (b) Evaluate  $\int_0^1 \frac{dx}{1+x^2}$  using Simpson's  $\frac{1}{3}$  rule taking  $h = \frac{1}{4}$ . 7

2. (a) From a pack of 52 cards, two are drawn one by one without replacement. Find the probability that both of them are kings. 7
- (b) Find the line of regression of  $y$  on  $x$  for the following data : 7

$x :$	10	9	8	7	6	4	3
$y :$	8	12	7	10	8	9	6

3. (a) If  $y = \sqrt{\frac{1-x}{1+x}}$  prove that 7
- $$(1-x^2)\frac{dy}{dx} + y = 0$$
- (b) If  $y = (\tan^{-1}x)^2$  show that 7
- $$(x^2+1)^2 y_2 + 2x(x^2+1) y_1 = 2$$
4. (a) Evaluate :  $\int \frac{x}{\sqrt{x+2}} dx$  7
- (b) Evaluate  $\int \frac{\sin 4x}{\sin x} dx$  7
5. (a) In a spherical triangle ABC, angle 7  
 $A = 124^\circ 21'$ , side  $AB = 41^\circ 30'$ , and side  
 $AC = 51^\circ 30'$ . Calculate side BC using  
haversine formula.
- (b) In a spherical right angled triangle angle 7  
 $B = 90^\circ$ , angle  $A = 43^\circ 30'$  and side  
 $a = 41^\circ 45'$ . Calculate sides b and c.
6. (a) Find the equation of the circle concentric 7  
with the circle  $x^2 + y^2 + 4x + 6y + 11 = 0$   
and passing through the point (5, 4).
- (b) Find the co-ordinates of the vertices, the foci, 7  
the eccentricity and the equation of  
directrices of the hyperbola  $16y^2 - 4x^2 = 1$ .